SPLICE RESEARCH
Progress Report
ANALYTICAL AND EXPERIMENTAL
INVESTIGATION OF THE MULTIPLE ROW EXTENDED 1/3
MOMENT END-PLATE CONNECTION
WITH EIGHT BOLTS AT THE
BEAM TENSION FLANGE
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ANALYTICAL AND EXPERIMENTAL INVESTIGATION
OF THE MULTIPLE ROW EXTENDED 1/3 MOMENT END-PLATE CONNECTION
WITH EIGHT BOLTS AT THE BEAM TENSION FLANGE

CHAPTER I

INTRODUCTION

1.1 Background

Moment end-plate connections are commonly used in steel portal frame construction as bolted moment-resistant connections. The moment end-plate is typically used to connect a beam to a beam, often referred to as a "splice-plate connection", Figure 1.1(a), or to connect a beam to a column, Figure 1.1(b).

Several design procedures for various moment end-plate configurations have been suggested to determine end-plate thickness and bolt diameter based on results from finite-element method, yield-line theory, or experimental test data. Unfortunately, these procedures produce a variety of values for end-plate thickness and bolt diameter for the same design example. For one particular configuration and loading, the variance of design end-plate thickness exceeded 100% [1]. An even greater variation was found for bolt force prediction, as some methods assume prying action is negligible, whereas other methods assume prying action is significant and contributes substantially to bolt force.
Hendrick et al [2] has finalized a unification of design procedures for four configurations of the flush type moment end-plate connection. Two of these flush type connections are unstiffened: the two-bolt unstiffened, Figure 1.2(a), and the four-bolt unstiffened, Figure 1.2(b). The other two flush type connections are stiffened: the four-bolt stiffened with web gusset plate between the two tension bolt rows, Figure 1.2(c), and the four-bolt stiffened with web gusset plate outside the two tension bolt rows, Figure 1.2(d). The gusset plates for each of the flush stiffened connections are symmetrical about the beam web and are welded to the end-plate and the beam web.

Morrison et al [3] has extended the unification of design procedures established by Hendrick et al [2] to a fifth configuration of moment end-plate. This configuration is the four-bolt extended stiffened form shown in Figure 1.3. In this connection, the four bolts in the tension region are placed one row of two bolts on each side of the beam tension flange. A triangular stiffener is located on the end-plate extension outside of the beam depth on the beam web centerline.

This report continues the unification of design procedures for moment end-plate connections established by Hendrick et al [2] and extended by Morrison et al [3] for another configuration of moment end-plate. This sixth configuration is the multiple row extended 1/3 form shown in Figure 1.4. In this connection, the eight bolts in the tension region are placed one row of two bolts outside the depth of the beam and three rows of two bolts inside the depth of the beam. The designation 1/3 reflects the number of bolt rows outside and inside, respectively, the beam depth at the beam tension flange. The unified design procedures include determination of end-plate thickness and prediction of bolt forces.
Figure 1.3  Four-Bolt Extended Stiffened Moment End-Plate Connection (Unification Extended by Morrison et al (3))

Figure 1.4  Multiple Row Extended 1/3 Moment End-Plate Connection
analytical prediction equations. Figure 1.5 presents the various parameters that define the end-plate geometry. These geometric parameters were varied within the limits shown in Table 1.1 to develop the experimental test matrix.
Table 1.1
Limits of Geometric Parameters

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<thead>
<tr>
<th>Parameter</th>
<th>Low (in)</th>
<th>Intermediate (in)</th>
<th>High (in)</th>
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<td>1-1/2</td>
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<tr>
<td>$P_b$</td>
<td>2</td>
<td>3-1/2</td>
<td>5</td>
</tr>
<tr>
<td>$g$</td>
<td>2-1/4</td>
<td>3-7/8</td>
<td>5-1/2</td>
</tr>
<tr>
<td>$h$</td>
<td>30</td>
<td>46</td>
<td>62</td>
</tr>
<tr>
<td>$b_f$</td>
<td>6</td>
<td>9</td>
<td>12</td>
</tr>
<tr>
<td>$t_w$</td>
<td>1/4</td>
<td>5/16</td>
<td>3/8</td>
</tr>
<tr>
<td>$t_f$</td>
<td>3/8</td>
<td>5/8</td>
<td>1</td>
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</tbody>
</table>
CHAPTER II
ANALYTICAL STUDY

2.1 Yield-Line Theory

Yield-lines are the continuous formation of plastic hinges along a straight or curved line. It is assumed that yield-lines divide a plate into rigid plane regions since elastic deformations are negligible when compared with plastic deformations. The failure mechanism of the plate exists when yield-lines form a kinematically valid collapse mechanism. Most of the yield-line theory development is related to reinforced concrete; nonetheless, the principles and findings are also applicable to steel plates.

The analysis of a yield-line mechanism can be performed by two different methods, the equilibrium method and the virtual work or energy method. The latter method is more suitable for the end-plate application and is used herein. In this method, the external work done by the applied load, in moving through a small arbitrary virtual deflection field, is equated to the internal work done as the plate rotates at the yield lines to facilitate this virtual deflection field. For a selected yield-line pattern and loading, a specific plastic moment is required along these hinge lines. For the same loading, other patterns may result in a larger required plastic moment capacity. Hence, the appropriate pattern is that which requires the largest required plastic moment. Conversely, for a given plastic moment capacity, the appropriate mechanism is that which produces the smallest failure load. This implies that the
Figure 2.1 Yield-Line Mechanisms for the Multiple Row Extended 1/3 Moment End-Plate Connection
A photo of an observed yield-line pattern for the multiple row extended 1/3 moment end-plate is shown in Figure 2.2. The yield-line pattern is indicated by the flaking of "white wash" from the test specimen.

2.2 Bolt Force Predictions

Yield-line theory does not produce bolt force predictions including prying action forces. Since experimental results indicate that prying action behavior is present in end-plate connections, a method suggested by Kennedy et al [4] was adopted to predict bolt forces as a function of applied flange force.

The Kennedy method is based on the split-tee analogy and three stages of plate behavior. Consider a split-tee model, Figure 2.3, consisting of a flange bolted to a rigid support and attached to a web through which a tension load is applied. At the lower levels of applied load, the flange behavior is termed thick plate behavior as plastic hinges have not formed in the split-tee flange, Figure 2.4(a). As the applied load is increased, two plastic hinges form at the centerline of the flange and each web face intersection, Figure 2.4(b). This yielding marks the "thick plate limit" and indicates the second stage of plate behavior termed intermediate plate behavior. At a greater applied load level, two additional plastic hinges form at the centerline of the flange and each bolt, Figure 2.4(c). The formation of this second set of plastic hinges marks the "thin plate limit" and indicates the third stage of plate behavior termed thin plate behavior.

For all stages of plate behavior, the Kennedy method predicts a bolt force as the sum of a portion of the applied force and a prying force. The portion of the applied force depends on the applied load, while the magnitude of the
Figure 2.3 Kennedy Method Split-Tee Model
Prying force depends on the stage of plate behavior. For the first stage of behavior, or thick plate behavior, the prying force is zero. For the second stage of behavior, or intermediate plate behavior, the prying force increases from zero at the thick plate limit to a maximum at the thin plate limit. For the third stage of behavior, or thin plate behavior, the prying force is maximum and constant. The distance "a" between the point of prying force application and the centerline of bolt has been determined empirically by Hendrick et al [2] for the flush end-plate configurations shown in Figure 1.2, as a function of $t_p/d_b$:

$$a = 3.682 \left( \frac{t_p}{d_b} \right)^3 - 0.085$$  \hspace{1cm} (2.7)

Modifications of the Kennedy method are necessary for application to the multiple row extended 1/3 moment end-plate connection. First, the connection is idealized in two parts: the outer end-plate and the inner end-plate, Figure 2.5. The outer end-plate consists of the end-plate extension outside the beam tension flange and a portion of the beam tension flange. The inner end-plate consists of the end-plate within the beam flanges and the remaining beam tension flange. Second, four factors: $\alpha$, $\beta_2$, $\beta_3$, and $\beta_4$, are introduced. These factors proportion the tension flange force to the outer end-plate, the $\alpha$, and inner end-plate, the $\beta_2$, $\beta_3$, and $\beta_4$. The factors were empirically developed as:

$$\alpha + \beta_2 + \beta_3 + \beta_4 \geq 1.0$$  \hspace{1cm} (2.8)

It was observed in five of six experimental tests (Chapter III) that no contact was made at the outside edges of the two outer end-plates in beam-to-beam connections. Since no contact was made, no prying action is possible. Thus, the outer end-plate behavior is thick at all applied load levels. The outer end-plate bolt force, $B_1$, is simply
the outer flange force, $\alpha F_f$, divided by the number of outer bolts, 2:

$$B_1 = \frac{\alpha F_f}{2}$$  \hfill (2.9)

The inner end-plate, on the other hand, does exhibit prying action at increased applied load levels in experimental testing. Two of the three inner bolt force are assumed to receive prying force contributions. The bolt force, $B_3$, not receiving prying force contributions is the second bolt force from the beam tension flange. Since the prying force is zero, the plate behavior is thick at all applied load levels. The bolt force, $B_3$, is simply a portion of the inner flange force, $\beta_3 F_f$, divided by the number of bolts, 2:

$$B_3 = \frac{\beta_3 F_f}{2}$$  \hfill (2.10)

The two bolt forces receiving prying force contributions are the bolt forces nearest to, $B_2$, and farthest from, $B_4$, the beam tension flange. In order to determine the magnitudes of these prying forces, and hence, the inner bolt forces, one must first ascertain the stages of inner end-plate behavior. The inner end-plate behavior is established by comparing the appropriate portion of the inner flange force, either $\beta_2 F_f$ or $\beta_4 F_f$, with the flange force at the thick plate limit $F_1$, and the flange force at the thin plate limit, $F_{11}$. The flange force at the thick plate limit, $F_1$, is:

$$F_1 = \frac{b_f t_p \sqrt{2F_{py}}}{4P_f \sqrt{1 + \left(3t_p^2/16P_f^2\right)}}$$  \hfill (2.11)

The flange force at the thin plate limit, $F_{11}$, is:
The \( F' \) term in the \( Q_{2\text{max}} \) expression is the lesser of:
\[
F_{\text{limit}} = \frac{F_1}{2} \quad (2.17)
\]
or
\[
F_{2\text{max}} = \beta_2 F_f / 2 \quad (2.18)
\]

Hence, the inner bolt force, \( B_2 \), for thin end-plate behavior is the inner flange force, \( \beta_2 F_f \), divided by the number of bolts, 2, plus the prying force, \( Q_{2\text{max}} \):
\[
B_2 = \frac{\beta_2 F_f}{2} + Q_{2\text{max}} \quad \text{when } \beta_2 F_f > F_1 \quad (2.19)
\]

An explanation of bolt force \( B_4 \) calculation parallels that for bolt force \( B_2 \). Nonetheless, bolt force \( B_4 \) equations are presented for completeness:
\[
B_4 = \frac{\beta_4 F_f}{2} \quad \text{when } \beta_4 F_f < F_1 \quad (2.20)
\]
\[
Q_4 = \frac{\beta_4 F_f P_f}{2a} - \frac{n d_b^3 F_y b}{32a} - \frac{b_f t_p^2}{8a} \sqrt{F_{p_y}^2 - 3(\frac{\beta_4 F_f}{b_f t_p})^2} \quad (2.21)
\]
\[
B_4 = \frac{\beta_4 F_f}{2} + Q_4 \quad \text{when } F_1 \leq \beta_4 F_f \leq F_{11} \quad (2.22)
\]
\[
Q_{4\text{max}} = \frac{w't_p^2}{4a} \sqrt{F_{p_y}^2 - 3(F' / w't_p)^2} \quad (2.23)
\]
\[
F' = \text{minimum} \quad | \quad F_{\text{limit}} = \frac{F_{11}}{2} \quad (2.24)
\]
\[
F_{4\text{max}} = \frac{\beta_4 F_f}{2} \quad (2.25)
\]
\[
B_4 = \frac{\beta_4 F_f}{2} + Q_{4\text{max}} \quad \text{when } \beta_4 F_f > F_{11} \quad (2.25)
\]

The reader is cautioned that the quantities under the radicals in Equations 2.14, 2.16, 2.21, and 2.23 can be
Figure 2.6 Typical $M-\phi$ Diagram
For beams, guidelines have been suggested [7,8] to correlate M-Φ connection behavior and AISC Construction Type. A Type I connection should carry an end moment greater than or equal to 90% of the full fixity end moment and not rotate more than 10% of the simple span rotation. A Type II connection should resist an end moment less than or equal to 20% of the full fixity end moment and rotate at least 80% of the simple span beam end rotation. A Type III connection lies between the limits of the Type I and Type II connections.

The simple span beam end rotation for any loading is given by:

\[ \Theta_s = \frac{M_F L}{2EI} \]  \hspace{1cm} (2.26)

Then, assuming \( M_F \) is the yield moment of the beam, \( SF_y \), and with \( I/S = h/2 \):

\[ \Theta_s = \frac{F_Y L}{E h} \]  \hspace{1cm} (2.27)

Taking as a limit \( L/h \) equal to 24, and with \( F_Y \) equal to 50 ksi and \( E \) equal to 29,000 ksi:

\[ 0.1\Theta_s = 0.00414 \text{ radians} \]  \hspace{1cm} (2.28)

This value is used in Section 4.3 to determine the suitability of the tested connections for Type I Construction.
CHAPTER III

EXPERIMENTAL INVESTIGATION

3.1 Test Setup and Procedure

A series of six tests were performed to verify the yield-line theory and modified Kennedy method predictions for the multiple row extended 1/3 moment end-plate connection. The test specimens consisted of end-plates welded to two beam sections which were in turn bolted together in the beam-to-beam connection configuration shown in Figure 3.1. Load was applied to the test specimen by a hydraulic ram via a load cell, swivel head, and spreader beam, as shown in Figure 3.2. The end-plates were subjected to pure moment as the test beam was simply supported and loaded with two equal concentrated loads symmetrically placed. Lateral support for both the test specimen and the spreader beam was provided by lateral brace mechanisms bolted to three steel wide flange frames anchored to the reaction floor of the laboratory.

Each test setup was instrumented with a load cell, three displacement transducers, a gaged caliper, a clip gage, four instrumented bolts, and twenty-six strain gages. Data was collected, processed, and recorded with an HP 3497A Data Acquisition/Control Unit and an HP 85 Computer. Real time plots of selected data were made with an HP 7470A Plotter permitting effective monitoring of the test.

The load cell measured the load applied by the
Figure 3.2 Test Setup Transverse Section
Strain Gage Location

B4
B3
B2
B1

Inner Bolts
Outer Bolts

Outer Plate Separation
Inner Plate Separation

2"

2/4

x/4

x/4

x/4

x/4

x/4

Note: Gaged bolts shown shaded

Figure 3.3 Location of Test Specimen Instrumentation
<table>
<thead>
<tr>
<th>Test Designation</th>
<th>$t_p$ (in)</th>
<th>$d_b$ (in)</th>
<th>$P_{ext}$ (in)</th>
<th>$P_f$ (in)</th>
<th>$P_b$ (in)</th>
<th>$8$ (in)</th>
<th>$h$ (in)</th>
<th>$b_f$ (in)</th>
<th>$t_w$ (in)</th>
<th>$t_f$ (in)</th>
<th>$F_{py}$ (ksi)</th>
<th>$b$ (ft)</th>
<th>$L$ (ft)</th>
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<tr>
<td>MRE1/3-3/4-3/8-30</td>
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<td>0.750</td>
<td>2.688</td>
<td>1.105</td>
<td>2.280</td>
<td>2.720</td>
<td>29.813</td>
<td>8.000</td>
<td>0.243</td>
<td>0.377</td>
<td>52.3</td>
<td>13.974</td>
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<td>1.000</td>
<td>3.404</td>
<td>1.567</td>
<td>3.019</td>
<td>4.574</td>
<td>30.003</td>
<td>8.063</td>
<td>0.260</td>
<td>0.377</td>
<td>50.1</td>
<td>13.935</td>
<td>40.000</td>
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<td>MRE1/3-7/8-7/16-46</td>
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<td>0.875</td>
<td>2.894</td>
<td>1.435</td>
<td>2.391</td>
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<td>15.987</td>
<td>44.089</td>
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<td>1.742</td>
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<td>46.026</td>
<td>8.241</td>
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<td>0.375</td>
<td>1.005</td>
<td>54.6</td>
<td>16.924</td>
<td>44.917</td>
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</table>
The second plot is end-plate separation versus applied moment. Both the inner and outer end-plate separation curves from the experimental test results are presented. The predicted ultimate moment from a yield-line analysis of the end-plate is also shown on this plot.

The third sheet contains two plots. Each plot is moment versus bolt force. The first plot contains two curves for the outer bolt force $B_1$: the modified Kennedy method prediction and the experimental test results. The second plot similarly contains two curves for the inner bolt force $B_2$: the modified Kennedy method prediction and the experimental test results. The predicted curves are plotted only for values less than or equal to the bolt proof load. Note that the "bolt force" plotted is a measured change in voltage divided by a calibration factor for a bolt. Since an instrumented bolt is calibrated only in the elastic range, measured "bolt force" is likewise only valid in the elastic range which is less than or equal to the bolt proof load. Actually, the plots represent the change in strain in the bolt shank.

The fourth sheet also contains two plots of moment versus bolt force. The first plot contains two curves for the inner bolt force $B_3$: the modified Kennedy method prediction and the experimental test results. The second plot similarly contains two curves for the inner bolt force $B_4$: the modified Kennedy method prediction and the experimental test results. The predicted curves are plotted only for values less than or equal to the bolt proof load.

The fifth and final sheet contains a single plot of moment versus rotation or $M-\Phi$ diagram. The $M-\Phi$ curve is developed by solving the following for the connection rotation, $\Phi$: 

-35-
Table 3.2
Tensile Coupon Test Results

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<th>Coupon</th>
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<th>Tensile Stress (ksi)</th>
<th>Elongation (%)</th>
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<td>59.4</td>
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<td>75.8</td>
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<td>76.0</td>
<td>75.0</td>
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</table>
CHAPTER IV

COMPARISON OF EXPERIMENTAL TEST RESULTS AND PREDICTIONS

4.1 End-Plate Strength Comparisons

The ultimate moment capacity for each experimental test specimen was calculated using Equation 2.3 or 2.5 as appropriate and the measured yield stress in Table 3.2. The maximum applied moment, predicted ultimate moment, and the ratio of predicted-to-applied moment for each experimental test are shown in Table 4.1. The predicted-to-applied moment ratios varied from 0.61 (more conservative) to 0.99 (less conservative). From the moment versus plate separation plots in the appendices, the predicted ultimate moment corresponds very closely to the yield plateau of each plate separation curve.

Two of the experimental tests, MRE1/3-1-1/2-30 and MRE1/3-7/8-7/16-46, were terminated at lower load levels than desired. Nonetheless, the behavior of these two tests closely corresponds to that observed for the remaining four experimental tests as shown by the moment versus plate separation curves.

4.2 Bolt Force Comparisons

Table 4.1 lists the applied and predicted moments at which bolt proof load was reached in the outer and inner bolts for each experimental test. The bolt proof load is
twice the allowable AISC Specification tension capacity. For A325 bolts, the proof load is calculated with 88 ksi and the bolt area based on nominal bolt diameter. Proof loads are 38.9 kips for 3/4 inch diameter bolts, 52.9 kips for 7/8 inch diameter bolts, 69.1 kips for 1 inch diameter bolts, 87.5 kips for 1-1/8 inch diameter bolts, 108.0 kips for 1-1/4 inch diameter bolts, and 155.5 kips for 1-1/2 inch diameter bolts. These values are shown on the moment versus bolt force plots in the appendices.

The predicted moments are obtained by determining values for the factors $\alpha$ in Equation 2.9; $\beta_2$ in Equations 2.13, 2.15, and 2.19; $\beta_3$ in Equation 2.10; and $\beta_4$ in Equations 2.20, 2.22, and 2.25. These factors proportion the beam tension flange force to the outer and inner end-plates. Factors $\alpha$, $\beta_2$, $\beta_3$, and $\beta_4$ were empirically determined from the experimental test data as:

$$\alpha = 0.60$$  (4.1)
$$\beta_2 = 0.35$$  (4.2)
$$\beta_3 = 0.45$$  (4.3)
$$\beta_4 = 0.25$$  (4.4)

Hence, $\alpha + \beta_2 + \beta_3 + \beta_4 = 1.65$.

In three of the four experimental tests for which comparative results are available, the inner bolt $B_2$ reached bolt proof load before outer bolt $B_1$. Considering the applied moments at which the inner bolt $B_2$ reached proof load, a $\beta_2 = 0.35$ was selected to best represent the experimental test data. The predicted-to-applied moment ratios for the inner bolt $B_2$ at proof load with $\beta_2 = 0.35$, range from 0.76 to 1.15. The experimental data show that the inner bolt $B_2$ force, actually a strain, increased at an increasing rate after the bolt proof load was reached. This indicates that the inner bolt $B_2$ was not accepting significant additional beam tension flange force.
CHAPTER V

DESIGN RECOMMENDATIONS AND EXAMPLE

5.1 Design Recommendations

This study continues the unification of design procedures for moment end-plate connections established by Hendrick et al [2] and extended by Morrison et al [3] to include a sixth configuration, the multiple row extended 1/3 moment end-plate connection. This unification provides consistent analytical procedures: end-plate strength criterion by yield-line theory and bolt force prediction by a modified Kennedy method. Further, an assessment of the connection rotational stiffness via M-\(\phi\) diagrams is presented. These analytical procedures are verified with adequate experimental testing.

The recommended design procedure follows:

1. Compute the factored beam end moment:

\[
M_u = M_w / 0.6 \tag{5.1}
\]

2. Establish values to define the end-plate geometry:

\(b_f, g, h, P_t, P_f, P_b, d_e,\) and \(t_w.\)

3. With a known yield stress, \(F_{py},\) determine the required end-plate thickness using the flow chart in Figure 5.1.
\[ \alpha = 0.60 \]
\[ \beta_2 = 0.35 \]
\[ a = 3.682 \left( \frac{t_p}{d_b} \right)^3 - 0.085 \]
\[ F_f = \frac{M_u}{(h - t_f)} \]
\[ F_1 = \frac{b_f t_p^2 F_{py}}{4p_f \sqrt{1 + \left( \frac{3t_p^2}{16p_f^2} \right)}} \]
\[ F_{11} = \frac{t_p^2 F_{py} \left[ 0.85(b_f/2) + 0.80 w' \right] + \left[ (nd_b^3 F_{yb}) / 8 \right]}{2p_f} \]

Figure 5.2 Flowchart to Determine Controlling Bolt Force
4. Select a trial bolt diameter and compute the controlling bolt force using the flowchart in Figure 5.2.

5. The required bolt diameter is determined from:

\[ d_b = \sqrt{\frac{2B_c}{\pi F_a}} \]  \hspace{1cm} (5.2)

where \( F_a \) = the allowable stress for the bolt material.

In the AISC Specification [5], the allowable tensile stress for A325 bolt material is 44 ksi with a factor of safety against yielding of 2.0. Equation 5.2 reflects this factor of safety.

Geometric limitations for the design procedure are found in Table 1.1. This procedure is demonstrated in Section 5.2.

5.2 Design Example

Determine the required end-plate thickness and bolt size for a multiple row extended 1/3 moment end-plate connection given the following:

Beam data...
A572 Gr 50 material
Depth
Flange width
Web thickness
Flange thickness

End-plate data...
A572 Gr 50 material
Extension outside beam flange

\( F_y = 50 \text{ ksi} \)
\( h = 62 \text{ in} \)
\( b_f = 10 \text{ in} \)
\( t_w = 3/8 \text{ in} \)
\( t_f = 1 \text{ in} \)

\( F_{py} = 50 \text{ ksi} \)
\( p_{ext} = 4-1/4 \text{ in} \)
\[ t_p = \left\{ \frac{M_u/F_{PY}}{(b_f/2)[1/2 + h/p_f + (h - p_c)/p_f + (h - p_{t3})/u]} \right\}^{\frac{1}{2}} + (2/g)(p_f + p_{b1,3} + u)(h - p_t) \]

\[ = \left\{ \frac{1166.7(12)/50}{(10/2)[1/2 + 62/2.375 + (62 - 2.375)/2.375 + (62 - 10.375)/3.15]} + 2/4.5(2.375 + 7.0 + 3.15)(62 - 3.375) \right\}^{\frac{1}{2}} \]

\[ = 0.649 \text{ in.} \]

**Step 3.** Determine \( u \) and required end-plate thickness for Mechanism 2.

\[ u = (1/2) \sqrt{b_f g} \]

\[ = (1/2) \sqrt{10(4.5)} = 3.35 \text{ in.} \]

\[ t_p = \left\{ \frac{M_u/F_{PY}}{(b_f/2)[1/2 + h/p_f + (h - p_c)/p_f + (h - p_{t3})/u]} \right\}^{\frac{1}{2}} + (2/g)(p_f + p_{b1,3})(h - t_f) + (2u/g)(h - p_{t3}) + (g/2) \]
Step 7. Determine inner end-plate behavior.

\[ F_1 = \frac{b_f t^2_p F_{py}}{4p_f \sqrt{1 + (3t^2_p/16p^2_f)}} \]

\[ = \frac{10(0.688)^2(50)}{4(2.375)\sqrt{1 + [3(0.688)^2/16(2.375)^2]}} = 24.7 \text{ kips} \]

Try 1 in. diameter bolts.

\[ w' = (b_f/2) - [d_b - (1/16)] \]

\[ = (10/2) - [1.0 - (1/16)] = 4.06 \text{ in.} \]

\[ F_{11} = \frac{t^2_p F_{py} [0.85(b_f/2) + 0.80w'] + [\pi d_b^3 F_{yb})/8]}{2p_f} \]

\[ = \frac{(0.688)^2 50[0.85(10/2) + 0.80(4.06)] + [\pi(1.0)^3(88)/8]}{2(2.375)} \]

\[ = 44.6 \text{ kips} \]

Since \( \beta_2 F_f = 0.35(229.5) = 80.3 \text{ kips} > F_{11} = 44.6 \text{ kips}, \)
inner end-plate behavior is thin.

Step 8. Determine inner bolt \( B_2 \) force.

\[ a = 3.682 \left(\frac{t_p}{d_b}\right)^3 - 0.085 \]

\[ = 3.682 \left(\frac{0.688}{1.0}\right)^3 - 0.085 = 1.114 \text{ in.} \]

-50-
Summary. For materials, geometry, and given loading, use A572 Gr 50 end-plate with 11/16 in. thickness and 1 in. diameter A325 bolts.
REFERENCES


APPENDIX A

NOMENCLATURE
NOMENCLATURE

\( a \) = distance from bolt centerline to prying force for plate

\( B \) = bolt force

\( B_1 \) = outer bolt force

\( B_2 \) = inner bolt force; first bolt from beam tension flange

\( B_3 \) = inner bolt force; second bolt from beam tension flange

\( B_4 \) = inner bolt force; third bolt from beam tension flange

\( b \) = distance from concentrated load to support for test specimen

\( b_f \) = beam flange width

\( d_b \) = bolt diameter

\( d_e \) = distance from bolt centerline to edge of end-plate extension

\( E \) = Young's modulus of elasticity

\( F \) = force

\( F_a \) = bolt material allowable stress

\( F_f \) = flange force

\( = M_u / (h - t_f) \)

\( F_{\text{limit}} \) = possible flange force per bolt at the thin plate limit

\( F_{\text{max}} \) = possible flange force per bolt at the thin plate limit

\( F_{\text{pY}} \) = plate material yield stress

\( F_Y \) = yield stress
\( P_t \) = distance from bolt centerline \( B_2 \) to far face of beam flange
\( = P_f + t_f \)

\( P_{t2} \) = distance from bolt centerline \( B_3 \) to far face of beam flange
\( = P_t + P_b \)

\( P_{t3} \) = distance from bolt centerline \( B_4 \) to far face of beam flange
\( = P_t + 2P_b \)

\( Q \) = prying force

\( Q_{max} \) = maximum prying force

\( Q_2 \) = prying force for bolt \( B_2 \)

\( Q_{2max} \) = maximum prying force for bolt \( B_2 \)

\( Q_4 \) = prying force for bolt \( B_4 \)

\( Q_{4max} \) = maximum prying force for bolt \( B_4 \)

\( S \) = section modulus

\( t_f \) = beam flange thickness

\( t_p \) = end-plate thickness

\( t_w \) = beam web thickness; stiffener thickness

\( t_1 \) = plate thickness at thick plate limit

\( t_{11} \) = plate thickness at thin plate limit

\( u \) = distance from bolt centerline \( B_4 \) to outermost yield-line

\( w \) = end-plate width per bolt pair

\( w' \) = end-plate width per bolt less bolt hole diameter (at bolt line)

\( x \) = distance

\( \alpha \) = outer end-plate factor

\( \beta_2 \) = inner end-plate factor for bolt \( B_2 \)

\( \beta_3 \) = inner end-plate factor for bolt \( B_3 \)

\( \beta_4 \) = inner end-plate factor for bolt \( B_4 \)

\( \delta_{\text{pred}} \) = predicted strength of materials centerline deflection for test specimen

\( \delta_{\text{test}} \) = experimental test centerline deflection for test specimen

\( \Theta_s \) = simple span end rotation for any loading

\( \pi \) = pi

\( \phi \) = rotation
APPENDIX B

MREL/3-3/4-3/8-30 TEST RESULTS
TEST SYNOPSIS

MBMA END-PLATE
MRE1/3-3/4-3/8-30
10-2-85
Multiple row extended 1/3 moment end-plate with a single row of two bolts outside and three rows of two bolts inside the beam tension flange

BEAM DATA:
Depth
Flange width
Web thickness
Flange thickness
Moment of inertia

h (in) = 29.813
bf (in) = 8.000
tw (in) = 0.243
tf (in) = 0.377
I (in**4) = 1876.2

END-PLATE:
Thickness
Extension outside beam flange
Pitch to bolt from flange
Pitch between bolt rows
Gage
Steel yield stress

tp (in) = 0.377
pext (in) = 2.688
pf (in) = 1.105
pb (in) = 2.280
g (in) = 2.720
Fpy (in) = 52.3

BOLT DATA:
Type
Diameter
Pretension force

db (in) = 0.750
Tb (k) = 28.0

PREDICTION:
End-plate failure moment
Bolt failure (proof) moment
Beam failure moment

Mu (k-ft) = 325.6
Myb (k-ft) = 318.1
Beam failure moment (k-ft) = 527.8

EXPERIMENTAL:
Maximum applied moment
Moment at bolt proof load
Maximum vertical centerline deflection
Maximum inner end-plate separation
Maximum outer end-plate separation

(k-ft) = 404.9
(k-ft) = 297.5
(in) = 3.214
(in) = 0.0867
(in) = 0.0321

DISCUSSION:
(c) Outer Bolt Force $B_1$ versus End-Plate Moment

(d) Inner Bolt Force $B_2$ versus End-Plate Moment

Figure B.1 Results from Test MRE1/3-3/4-3/8-30, Continued B.3
(g) End-Plate Moment versus Rotation

Figure B.1 Results from Test MRE1/3-3/4-3/8-30, Continued
APPENDIX C

MRE1/3-1-1/2-30 TEST RESULTS
## TEST SYNOPSIS

**PROJECT:**

**TEST:**

**TEST DATE:**

**CONNECTION DESCRIPTION:**

**BEAM DATA:**

<table>
<thead>
<tr>
<th>Depth</th>
<th>h (in)</th>
<th>= 30.003</th>
</tr>
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<tbody>
<tr>
<td>Flange width</td>
<td>bf (in)</td>
<td>= 8.063</td>
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<tr>
<td>Web thickness</td>
<td>tw (in)</td>
<td>= 0.260</td>
</tr>
<tr>
<td>Flange thickness</td>
<td>tf (in)</td>
<td>= 0.377</td>
</tr>
<tr>
<td>Moment of inertia</td>
<td>I (in**4)</td>
<td>= 1876.2</td>
</tr>
</tbody>
</table>

**END-PLATE:**

| Thickness | tp (in) | = 0.501 |
| Extension outside beam flange | pext (in) | = 3.404 |
| Pitch to bolt from flange | pf (in) | = 1.567 |
| Pitch between bolt rows | pb (in) | = 3.019 |
| Gage | g (in) | = 4.574 |
| Steel yield stress | Fpy (in) | = 50.1 |

**BOLT DATA:**

| Type | = A325 |
| Diameter | db (in) | = 1.000 |
| Pretension force | Tb (k) | = 51.0 |

**PREDICTION:**

| End-plate failure moment | Mu (k-ft) | = 258.9 |
| Bolt failure (proof) moment | Myb (k-ft) | = 570.0 |
| Beam failure moment | = 523.2 |

**EXPERIMENTAL:**

| Maximum applied moment | (k-ft) | = 425.1 |
| Moment at bolt proof load | (k-ft) | = ------ |
| Maximum vertical centerline deflection | (in) | = 3.445 |
| Maximum inner end-plate separation | (in) | = 0.0383 |
| Maximum outer end-plate separation | (in) | = 0.0694 |

**DISCUSSION:**

A hydraulic problem occurred during the final test setup loading sequence. The test was terminated at lower load levels than anticipated.
(c) Outer Bolt Force B₁ versus End-Plate Moment

(d) Inner Bolt Force B₂ versus End-Plate Moment

Figure C.1 Results from Test MRE1/3-1-1/2-30, Continued C.3
(g) End-Plate Moment versus Rotation

Figure C.1 Results from Test MRE1/3-1-1/2-30, Continued
APPENDIX D

MRE1/3-7/8-7/16-46 TEST RESULTS
TEST SYNOPSIS

PROJECT:
TEST:
TEST DATE:
CONNECTION DESCRIPTION:

MBMA END-PLATE
MRE1/3-7/8-7/16-46
11-1-85
Multiple row extended 1/3 moment end-
plate with a single row of two bolts
outside and three rows of two bolts
inside the beam tension flange

BEAM DATA:
Depth
Flange width
Web thickness
Flange thickness
Moment of inertia

h (in) = 45.994
bf (in) = 8.112
tw (in) = 0.353
tf (in) = 0.495
I (in**4) = 6834.0

END-PLATE:
Thickness
tp (in) = 0.445
Extension outside beam flange pext (in) = 2.894
Pitch to bolt from flange pf (in) = 1.435
Pitch between bolt rows pb (in) = 2.391
g (in) = 3.253
Gage
Steel yield stress Fpy (in) = 62.1

BOLT DATA:
Type
Diameter db (in) = 0.875
Pretension force Tb (k) = 39.0

PREDICTION:
End-plate failure moment Mu (k-ft) = 570.0
Bolt failure (proof) moment Myb (k-ft) = 643.5
Beam failure moment

EXPERIMENTAL:
Maximum applied moment (k-ft) = 866.1
Moment at bolt proof load (k-ft) = 838.8
Maximum vertical centerline deflection (in) = 1.802
Maximum inner end-plate separation (in) = 0.0345
Maximum outer end-plate separation (in) = 0.0540

DISCUSSION:
A local buckle occurred adjacent the end-plate in the beam compression
flange. The test was terminated at lower load levels than anticipated.

D.1
(c) Outer Bolt Force $B_1$ versus End-Plate Moment

(d) Inner Bolt Force $B_2$ versus End-Plate Moment

Figure D.1 Results from Test MRE1/3-7/8-7/16-46, Continued D.3
(g) End-Plate Moment versus Rotation

Figure D.1 Results from Test MRE1/3-7/8-7/16-46, Continued
APPENDIX E

MRE1/3-1 1/8-5/8-46 TEST RESULTS
TEST SYNOPSIS

PROJECT: MBMA END-PLATE
TEST: MRE1/3-1 1/8-5/8-46
TEST DATE: 11-12-85
CONNECTION DESCRIPTION: Multiple row extended 1/3 moment end-plate with a single row of two bolts outside and three rows of two bolts inside the beam tension flange

BEAM DATA:
- Depth: h (in) = 46.026
- Flange width: bf (in) = 8.241
- Web thickness: tw (in) = 0.386
- Flange thickness: tf (in) = 0.498
- Moment of inertia: I (in**4) = 7186.8

END-PLATE:
- Thickness: tp (in) = 0.634
- Extension outside beam flange: pext (in) = 3.815
- Pitch to bolt from flange: pf (in) = 1.742
- Pitch between bolt rows: pb (in) = 3.020
- Gage: g (in) = 3.949
- Steel yield stress: Fpy (in) = 57.2

BOLT DATA:
- Type: 
- Diameter: db (in) = 1.125
- Pretension force: Tb (k) = 56.0

PREDICTION:
- End-plate failure moment: Mu (k-ft) = 966.7
- Bolt failure (proof) moment: Myb (k-ft) = 1106.6
- Beam failure moment

EXPERIMENTAL:
- Maximum applied moment: (k-ft) = 975.1
- Moment at bolt proof load: (k-ft) = ------
- Maximum vertical centerline deflection: (in) = 1.940
- Maximum inner end-plate separation: (in) = 0.0082
- Maximum outer end-plate separation: (in) = 0.0153

DISCUSSION:
(c) Outer Bolt Force $B_1$ versus End-Plate Moment

(d) Inner Bolt Force $B_2$ versus End-Plate Moment

Figure E.1 Results from Test MRE1/3-1 1/8-5/8-46, Continued

E.3
(f) End-Plate Moment versus Rotation

Figure E.1 Results from Test MRE1/3-1 1/8-5/8-46, Continued
APPENDIX F

MRE1/3-1  1/4-5/8-62  TEST RESULTS
TEST SYNOPSIS

PROJECT: MBMA END-PLATE
TEST: MRE1/3-1 1/4-5/8-62
TEST DATE: 12-6-85
CONNECTION DESCRIPTION: Multiple row extended 1/3 moment end-plate with a single row of two bolts outside and three rows of two bolts inside the beam tension flange

BEAM DATA:

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<th>Property</th>
<th>Symbol</th>
<th>Unit</th>
<th>Value</th>
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<tr>
<td>Depth</td>
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<tr>
<td>Flange width</td>
<td>bf</td>
<td>(in)</td>
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<td>Web thickness</td>
<td>tw</td>
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<tr>
<td>Flange thickness</td>
<td>tf</td>
<td>(in)</td>
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<tr>
<td>Moment of inertia</td>
<td>I</td>
<td>(in**4)</td>
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END-PLATE:

<table>
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<th>Symbol</th>
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<tr>
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<td>tp</td>
<td>(in)</td>
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<tr>
<td>Extension outside beam flange</td>
<td>pext</td>
<td>(in)</td>
<td>4.225</td>
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<td>Pitch to bolt from flange</td>
<td>pf</td>
<td>(in)</td>
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<td>Pitch between bolt rows</td>
<td>pb</td>
<td>(in)</td>
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<td>Gage</td>
<td>g</td>
<td>(in)</td>
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<td>Steel yield stress</td>
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BOLT DATA:

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<td>Pretension force</td>
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PREDICTION:

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<td>End-plate failure moment</td>
<td>Mu</td>
<td>(k-ft)</td>
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<tr>
<td>Bolt failure (proof) moment</td>
<td>Myb</td>
<td>(k-ft)</td>
<td>1690.6</td>
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<tr>
<td>Beam failure moment</td>
<td></td>
<td>(k-ft)</td>
<td>3681.6</td>
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EXPERIMENTAL:

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<td>Moment at bolt proof load</td>
<td>(k-ft)</td>
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<td>Maximum vertical centerline deflection</td>
<td>(in)</td>
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<td>Maximum inner end-plate separation</td>
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<tr>
<td>Maximum outer end-plate separation</td>
<td>(in)</td>
<td>0.572</td>
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DISCUSSION:

F.1
(c) Outer Bolt Force $B_1$ versus End-Plate Moment

(d) Inner Bolt Force $B_2$ versus End-Plate Moment

Figure F.1  Results from Test MRE1/3-1 1/4-5/8-62, Continued F.3
(g) End-Plate Moment versus Rotation

Figure F.1 Results from Test MREI/3-1 1/4-5/8-62, Continued
APPENDIX G

MRE1/3-1 1/2-3/4-62 TEST RESULTS
**TEST SYNOPSIS**

**PROJECT:**

**TEST:**

**TEST DATE:**

**CONNECTION DESCRIPTION:**

**BEAM DATA:**

<table>
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<td>Web thickness</td>
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<td>Flange thickness</td>
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**END-PLATE:**

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<th>Thickness</th>
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<td>pext</td>
<td>(in)</td>
<td>5.130</td>
</tr>
<tr>
<td>Pitch to bolt from flange</td>
<td>pf</td>
<td>(in)</td>
<td>2.584</td>
</tr>
<tr>
<td>Pitch between bolt rows</td>
<td>pb</td>
<td>(in)</td>
<td>4.516</td>
</tr>
<tr>
<td>Gage</td>
<td>g</td>
<td>(in)</td>
<td>5.559</td>
</tr>
<tr>
<td>Steel yield stress</td>
<td>Fpy</td>
<td>(in)</td>
<td>54.6</td>
</tr>
</tbody>
</table>

**BOLT DATA:**

<table>
<thead>
<tr>
<th>Type</th>
<th></th>
<th></th>
<th>A325</th>
</tr>
</thead>
<tbody>
<tr>
<td>Diameter</td>
<td>db</td>
<td>(in)</td>
<td>1.500</td>
</tr>
<tr>
<td>Pretension force</td>
<td>Tb</td>
<td>(k)</td>
<td>103.0</td>
</tr>
</tbody>
</table>

**PREDICTION:**

<table>
<thead>
<tr>
<th>End-plate failure moment</th>
<th>Mu</th>
<th>(k-ft)</th>
<th>1601.6</th>
</tr>
</thead>
<tbody>
<tr>
<td>Bolt failure (proof) moment</td>
<td>Myb</td>
<td>(k-ft)</td>
<td>2575.2</td>
</tr>
<tr>
<td>Beam failure moment</td>
<td></td>
<td></td>
<td>3717.8</td>
</tr>
</tbody>
</table>

**EXPERIMENTAL:**

| Maximum applied moment     | (k-ft) | 2329.6 |
| Moment at bolt proof load   | (k-ft) | 2221.8 |
| Maximum vertical centerline deflection | (in) | 1.499 |
| Maximum inner end-plate separation | (in) | 0.0512 |
| Maximum outer end-plate separation | (in) | 0.1146 |

**DISCUSSION:**

G.1
(c) Outer Bolt Force B1 versus End-Plate Moment

(d) Inner Bolt Force B2 versus End-Plate Moment

Figure G.1 Results from Test MRE1/3-1 1/2-3/4-62, Continued 6.3
(g) End-Plate Moment versus Rotation

Figure G.1 Results from Test MRE1/3-1 1/2-3/4-62, Continued