



## A novel rolling horizon strategy for the strategic planning of supply chains. Application to the sugar cane industry of Argentina

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### ARTICLE INFO

#### Article history:

Received 10 April 2010

Received in revised form 10 January 2011

Accepted 12 April 2011

Available online 22 April 2011

#### Keywords:

Supply chain management (SCM)

Bioethanol

Sugar cane industry

Rolling horizon

### ABSTRACT

In this article, we propose a new method to reduce the computational burden of strategic supply chain (SC) planning models that provide decision support for public policy makers. The method is based on a rolling horizon strategy where some of the integer variables in the mixed-integer programming model are treated as continuous. By comparing with rigorous solutions, we show that the strategy works efficiently. We illustrate the capabilities of the approach presented by its application to a SC design problem related to the sugar cane industry in Argentina. The case study involves determining the number and type of production and storage facilities to be built in each region of the country so that the ethanol and sugar demand is fulfilled and the economic performance is maximized.

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### 1. Introduction

Supply chain management (SCM) has recently gained wider interest in both, academia and industry, given its potential to increase the benefits through an efficient coordination of the operations of supply, manufacturing and distribution carried out in a network (Narahariseti, Adhitya, Karimi, & Srinivasan, 2009; Puigjaner & Guillén-Gosálbez, 2008). In the context of process systems engineering (PSE), these activities are the focus of the emerging area known as Enterprise Wide Optimization (EWO), which as opposed to SCM, places more emphasis on the manufacturing stage (Grossmann, 2005).

The SCM problem may be considered at different levels depending on the strategic, tactical, and operational variables involved in the decision-making process (Fox, Barbuceanu, & Teigen, 2000). The strategic level is based on those decisions that have a long-lasting effect on the firm. These include, among many others, the SC design problem, which addresses the optimal configuration of an entire SC network. The tactical level encompasses long- to medium-term management decisions, which are typically updated a few times every year, and include overall purchasing and production

decisions, inventory policies, and transport strategies. Finally, the operational level refers to day-to-day decisions such as scheduling, lead-time quotations, routing, and lorry loading (Guillén-Gosálbez, Espuña, & Puigjaner, 2006).

In the recent past the SCM tools developed in these hierarchical levels have primarily focused on maximizing the economic performance in the private sector. By contrast, the academic literature on SCM applications for public policy makers is still quite scarce (see Preuss, 2009). The use of SCM tools in the latter area is very promising, since they can provide valuable insight into how to satisfy the population's needs in an efficient manner, thus guiding government authorities towards the adoption of the best technological alternatives to be promoted and eventually established in a given country.

The goal of this paper is to provide a general modeling framework and a solution strategy for SC design problems, with focus on the strategic level of SCM, and with special emphasis on applications found in the public sector. Particularly, given a set of available production, storage and transportation technologies that can be adopted in different regions of a country, the goal of the analysis performed is to determine the optimal SC configuration, including the type of technologies selected, the capacity expansions over time, and their optimal location, along with the associated planning decisions that maximize a given economic criterion. In this work, such a design task is formulated in mathematical terms as a mixed-integer programming problem with a specific structure that includes integer and binary variables of different nature. To

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**Nomenclature***Indices*

|     |                            |
|-----|----------------------------|
| $i$ | materials                  |
| $g$ | sub-region zones           |
| $l$ | transportation modes       |
| $p$ | manufacturing technologies |
| $s$ | storage technologies       |
| $t$ | time periods               |

*Sets*

|         |  |
|---------|--|
| $IL(l)$ | set of materials that can be transported via transportation mode $l$ |
| $IM(p)$ | set of main products for each technology $p$                         |
| $IS(s)$ | set of materials that can be stored via storage technology $s$       |
| $LI(i)$ | set of transportation modes $l$ that can transport material $i$      |
| $SEP$   | set of products that can be sold                                     |
| $SI(i)$ | set of storage technologies that can store materials $i$             |

*Parameters*

|                       |  |
|-----------------------|--|
| $\alpha_{pgt}^{PL}$   | fixed investment coefficient for technology $p$                        |
| $\alpha_{sgt}^S$      | fixed investment coefficient for storage technology $s$                |
| $\beta$               | storage period   |
| $\beta_{pgt}^{PL}$    | variable investment coefficient for technology $p$                     |
| $\beta_{sgt}^S$       | variable investment coefficient for storage technology $s$             |
| $\rho_{pi}$           | material balance coefficient of material $i$ in technology $p$         |
| $\tau$                | minimum desired percentage of the available installed capacity         |
| $\varphi$             | tax rate   |
| $avl_l$               | availability of transportation mode $l$                                |
| $CapCrop_{gt}$        | total capacity of sugar cane plantations in sub-region $g$ in time $t$ |
| $DW_{lt}$             | driver wage  |
| $EL_{gg'}$            | distance between $g$ and $g'$  |
| $\overline{FCI}$      | upper limit for capital investment                                     |
| $FE_l$                | fuel consumption of transport mode $l$                                 |
| $FP_{lt}$             | fuel price   |
| $GE_{lt}$             | general expenses of transportation mode $l$                            |
| $LT_{ig}$             | landfill tax   |
| $ME_l$                | maintenance expenses of transportation mode $l$                        |
| $\overline{PCap}_p$   | maximum capacity of technology $p$                                     |
| $\underline{PCap}_p$  | minimum capacity of technology $p$                                     |
| $\overline{PR}_{igt}$ | prices of final products   |
| $\overline{Q}_l$      | maximum capacity of transportation mode $l$                            |
| $\underline{Q}_l$     | minimum capacity of transportation mode $l$                            |
| $\overline{SCap}_s$   | maximum capacity of technology $p$                                     |
| $\underline{SCap}_s$  | minimum capacity of storage technology $s$                             |
| $\overline{SD}_{igt}$ | actual demand of product $i$ in sub-region $g$ in time $t$             |
| $SP_l$                | average speed of transportation mode $l$                               |
| $sv$                  | salvage value  |
| $T$                   | number of time intervals   |
| $TCap_l$              | capacity of transportation mode $l$                                    |
| $TMC_{lt}$            | cost of establishing transportation mode $l$ in period $t$             |
| $UPC_{ipgt}$          | unit production cost   |
| $USC_{isgt}$          | unit storage cost  |

*Variables*

|               |   |
|---------------|---|
| $CF_t$        | cash flow in time $t$   |
| $DC_t$        | disposal cost in time $t$   |
| $DTS_{igt}$   | delivered amount of material $i$ in sub-region $g$ in period $t$  |
| $FC_t$        | fuel cost   |
| $FCI$         | fixed capital investment  |
| $FOC_t$       | facility operating cost in time $t$   |
| $FTDC_t$      | fraction of the total depreciable capital in time $t$   |
| $GC_t$        | general cost  |
| $LC_t$        | labor cost  |
| $MC_t$        | maintenance cost  |
| $NE_t$        | net earnings in time $t$  |
| $NP_{pgt}$    | number of installed plants with technology $p$ in sub-region $g$ in time $t$  |
| $NPV$         | net present value of SC   |
| $NS_{sgt}$    | number of installed storages with storage technology $s$ in sub-region $g$ in time $t$                                    |
| $NT_{lt}$     | number of transportation units $l$  |
| $PCap_{pgt}$  | existing capacity of technology $p$ in sub-region $g$ in time $t$   |
| $PCapE_{pgt}$ | expansion of the existing capacity of technology $p$ in sub-region $g$ in time $t$  |
| $Q_{ilgg't}$  | flow rate of material $i$ transported by mode $l$ from sub-region $g'$ to current sub-region $g$ in time period $t$       |
| $Rev_t$       | revenue in time $t$   |
| $RNP_{pgt}$   | "relaxed" number of installed plants with technology $p$ in sub-region $g$ in time interval $t$                           |
| $RNS_{sgt}$   | "relaxed" number of installed storages with storage technology $s$ in sub-region $g$ in time interval $t$                 |
| $RNT_{lt}$    | "relaxed" number of transportation units $l$ in time interval $t$   |
| $SCap_{sgt}$  | capacity of storage $s$ in sub-region $g$ in time $t$   |
| $SCapE_{sgt}$ | expansion of the existing capacity of storage $s$ in sub-region $g$ in time $t$   |
| $ST_{isgt}$   | total inventory of material $i$ in sub-region $g$ stored by technology $s$ in time $t$                                    |
| $TOC_t$       | transport operating cost in time $t$  |
| $PE_{ipgt}$   | production rate of material $i$ in technology $p$ in sub-region $g$ in time $t$   |
| $PT_{igt}$    | total production rate of material $i$ in sub-region $g$ in time $t$   |
| $PU_{igt}$    | purchase of material $i$ in sub-region $g$ in time $t$  |
| $X_{lgg't}$   | binary variable, which is equal to 1 if material flow between two sub-regions $g$ and $g'$ is established and 0 otherwise |
| $W_{igt}$     | amount of wastes $i$ generated in sub-region $g$ in period $t$  |

expedite the solution of such formulation, we propose a novel decomposition method based on a customized "rolling horizon" algorithm that achieves significant reductions in CPU time while still providing near optimal solutions.

The paper is organized as follows. First, a literature review on strategic SCM tools based on mathematical programming is presented, followed by a more specific review on the particular application of these techniques to the sugar cane industry. A formal definition of the problem under study is given next along with its mathematical formulation. The following section introduces a tailor-made decomposition strategy that reduces the computational burden of the model by exploiting its mathematical structure. The capabilities of the proposed modeling framework and solution

strategy are illustrated next through a case study based on the sugar cane industry of Argentina. The conclusions of the work are finally drawn in the last section of the paper.

### 1.1. Mathematical programming approaches for strategic SCM problems

Optimization using mathematical programming is probably the most widely used approach in SCM. General literature reviews can be found in the work by Mula, Peidro, Díaz-Madroñero, and Vicens (2010), whereas a more specific work devoted to process industries can be found in the articles by Grossmann (2005) and Papageorgiou (2009). The preferred modeling tool for addressing strategic SCM problems has been mixed-integer linear programming (MILP). MILP models for SCM typically adopt fairly simple aggregated representations of capacity that avoid nonlinearities. This feature has been the key of their success, since it has allowed them to be easily adapted to a wide range of industrial applications. In these MILP formulations, continuous variables are used to represent materials flows and purchases and sales of products, whereas binary variables are employed to model tactical and/or strategic decisions associated with the network configuration, such as selection of technologies and establishment of facilities and transportation links (Guillén-Gosálbez, Mele, Espuña, & Puigjaner, 2006; Laínez, Guillén-Gosálbez, Badell, Espuña, & Puigjaner, 2007).

Several solution strategies have been explored for effectively solving these strategic SCM problems. Bok, Grossmann, and Park (2000) reported an implementation of a bi-level decomposition algorithm to solve a MILP model that maximized the profit of a network showing that this algorithm could reduce the solution time by half compared to the full space method implemented in CPLEX. Guillén-Gosálbez, Mele, and Grossmann (2010) presented also a bi-level algorithm for solving the strategic planning of hydrogen SCs for vehicle use. Using numerical examples, they showed that the decomposition method could achieve a reduction of one order of magnitude in CPU time compared to the full space method (the whole model without decomposition, relaxation or approximations) while still providing near optimal solutions (i.e., with less than 1% of optimality gap).

Lagrangian decomposition has also been used in strategic SCM problems. Gupta and Maranas (1999) applied Lagrangian decomposition to solve a planning problem that considered different products and manufacturing sites. With this decomposition technique, the authors obtained a solution with an optimality gap of 1.6%, reducing in one order of magnitude the CPU time required by CPLEX 4.0 to find a solution with a gap of 3.2%. You and Grossmann (2010) introduced a spatial decomposition algorithm based on the integration of Lagrangian relaxation and piecewise linear approximation to reduce the computational expense of solving multi-echelon supply chain design problems in the presence of uncertain customer demands. Chen and Pinto (2008) investigated the application of various Lagrangian-based techniques including Lagrangian decomposition, Lagrangian relaxation, and Lagrangian/surrogate relaxation, coupled with subgradient and modified subgradient optimization. The comparison showed that the proposed strategies are much more efficient than the full space method. Particularly, they concluded that the computational time was greatly reduced while still achieving optimality gaps of less than 2%.

Other solution methods applied to SCM problems have been Bender's decomposition (Geoffrion & Graves, 1974) and "rolling horizon" algorithms based on the original work by Wilkinson (1996). The former approach has been mainly used in the context of strategic/tactical SCM problems (Cordeau, Pasin, & Solomon, 2006; Dogan & Goetschalckx, 1999; MirHassani, Lucas, Mitra, Messina, & Poojari, 2000; Paquet, Martel, & Desaulniers, 2004; Santoso,

Ahmed, Goetschalckx, & Shapiro, 2005; Uster, Easwaran, Akcali, & Cetinkaya, 2007), whereas the latter strategy has been typically applied to operational SCM problems (Dimitriadis, Shah, & Pantelides, 1997; Elkamel & Mohindra, 1999; Balasubramanian & Grossmann, 2004). Rolling horizon algorithms are based on approximating the solution of the full space model by a set of sub-models, each of which representing only part of the planning horizon in detail. This strategy has been shown to be very efficient in solving scheduling problems with large time horizons (Van den Heever & Grossmann, 2003). However, to our knowledge, it has never been applied to strategic SCM problems.

### 1.2. Applications of mathematical programming to the sugar cane industry

The interest in renewable fuels such as bioethanol and other bio-fuels has greatly increased in the last years all over the world. Following this trend, Argentina approved the National Act 26,093, which aims to promote the production of bioethanol for fuel blending. This new legislation represents a major challenge for the sugar cane industry, which must increase its flexibility and efficiency in order to satisfy the growing sugar and bioethanol demand. The final goal of this law is to promote the adoption of proper energetic and environmental policies.

The interest on ethanol has motivated the development of mathematical programming tools for optimizing its production. The models presented so far have mainly focused on studying the individual components of the ethanol SC rather than optimizing all its entities in an integrated manner. Particularly, Yoshizaki, Muscat, and Biazzi (1996) introduced a LP model to find the optimal distribution of sugar cane mills, fuel bases and consumer sites in southeastern Brazil. Kawamura, Ronconi, and Yoshizaki (2006) presented a LP model to minimize the transportation and external storage costs of the existing SC in Brazil. Ioannou (2005) applied a LP optimization model to reduce the transportation cost in the Greek sugar industry, while Milán, Fernández, and Pla Aragónés (2006) introduced a MILP model to minimize the transportation cost of a sugar cane SC in Cuba. Dunnett, Adjiman, and Shah (2008) developed a combined production and logistic model to find the optimal configuration of a lignocellulosic bioethanol SC. Mathematical programming methods associated with plantation planning and scheduling can be found in the works by Grunow, Guenther, and Westinner (2007), Paiva and Morabito (2009); Colin (2009) and Higgins and Laredo (2006).

As observed, most of the aforementioned approaches have focused on the tactical level of the SCM problem covering short/medium-term decisions associated with the SC operation. These methods consider a given SC configuration and attempt to optimize its activities without modifying the existing topology. A general modeling and solution framework for holistically optimizing ethanol infrastructures is currently lacking. Such an approach would enable governments to choose, in advance, the optimum configurations for ethanol production, storage and delivery systems. A systematic tool of this type could play a major role in guiding national and international policy makers towards the best decisions in the transition process from traditional fossil fuels to biofuels. In this article, we fill this research gap by proposing a novel mathematical formulation for the strategic planning of sugar cane SCs along with an efficient solution method that allows to tackle problems of realistic size in moderate CPU times.

## 2. Problem statement

To formally state the SC design problem, we consider a generic three-echelon SC (production–storage–market) like the

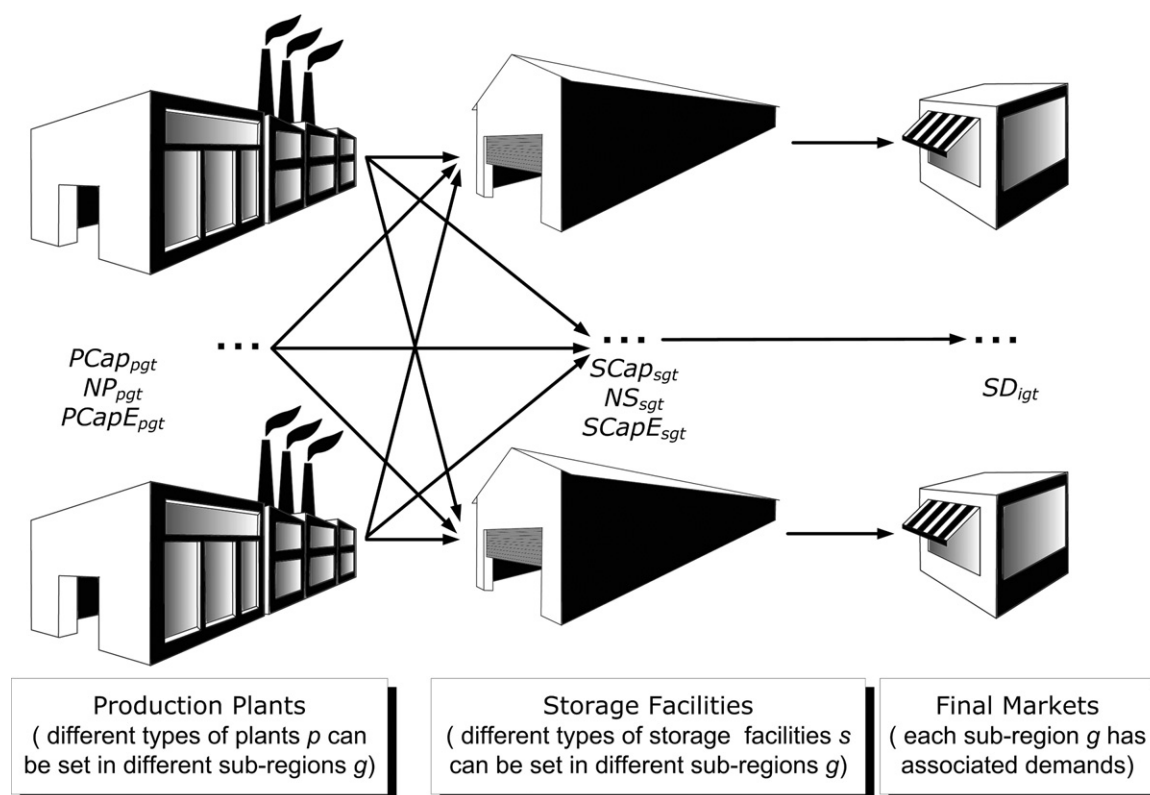


Fig. 1. Structure of the three-echelon ethanol/sugar SC.

one depicted in Fig. 1. This network includes a set of production and storage facilities, and final markets. We assume that we are given a specific region of interest that is divided into a set of sub-regions in which the facilities of the SC can be established in order to cover a given demand. In general, these sub-regions, which are regarded as potential locations for the SC entities, will be defined according to the administrative division of a country. The SC design problem can then be formally stated as follows.

Given are a fixed time horizon, product prices, cost parameters for production, storage and transportation of materials, demand forecast, tax rate, capacity data for plants, storages and transportation links, fixed capital investment data, interest rate, storage holding period and landfill tax. The goal is to determine the configuration of a three-echelon bioethanol network and associated planning decisions with the goal of maximizing the economic performance for a given time horizon. Decisions to be made include the number, location and capacity of production plants and warehouses to be set up in each sub-region, their capacity expansion policy for a given forecast of prices and demand over the planning horizon, the transportation links and transportation modes of the network, and the production rates and flows of feed stocks, wastes and final products.

### 3. Mathematical model

In this section, we present a mathematical model that considers the specific features of the sugar cane industry, while still being general enough to be easily adapted to any other industrial SC. Particularly, our model is based on the MILP formulation introduced by [Almansoori and Shah \(2006\)](#), and [Guillén-Gosálbez et al. \(2010\)](#), which addresses the design of hydrogen SCs. Furthermore, the model follows the SC formulation developed by [Guillén-Gosálbez and Grossmann](#) for the case of petrochemical SCs ([Guillén-Gosálbez](#)

& [Grossmann, 2009b](#); [Guillén-Gosálbez & Grossmann, 2010a](#)), in the way in which the mass balances are handled.

Compared to standard SC formulations that focus on the private sector, the model exhibits two main differentiating features. The first one is that plants, warehouses and final markets share the same potential locations. These locations correspond to the sub-regions in which the overall region of interest is divided. The second one is that the model accounts for the option of opening more than one facility in a given region and time period. This consideration requires the introduction of integer variables that increase the combinatorial complexity of the model. This structure is exploited by our solution algorithm.

As sugar and ethanol share the same feedstock, the proposed model includes integrated infrastructures for ethanol/sugar production. The mathematical formulation considers all possible configurations of the future ethanol/sugar SC as well as all technological aspects associated with the SC performance such as production and storage technologies, waste disposal, modes for transportation of raw materials, products and wastes. We describe next some general features of the model before immersion into a detailed description of its equations.

#### Production plants

Sugar cane is the leading feedstock for bioethanol production in Argentina as well as in most of the tropical regions all over the world (e.g., Brazil, India, China, etc.). The juice is extracted from sugar cane mainly by milling. From this step sugar cane juice can be treated in different ways. Sugar factories can use this juice to produce white sugar and raw sugar. There are two technologies realizing the “sugar cane-to-sugar” pathway: one of them generates molasses (T1) as a byproduct, whereas the other one provides a secondary honey (T2) in addition to sugars. These two kinds of byproducts are

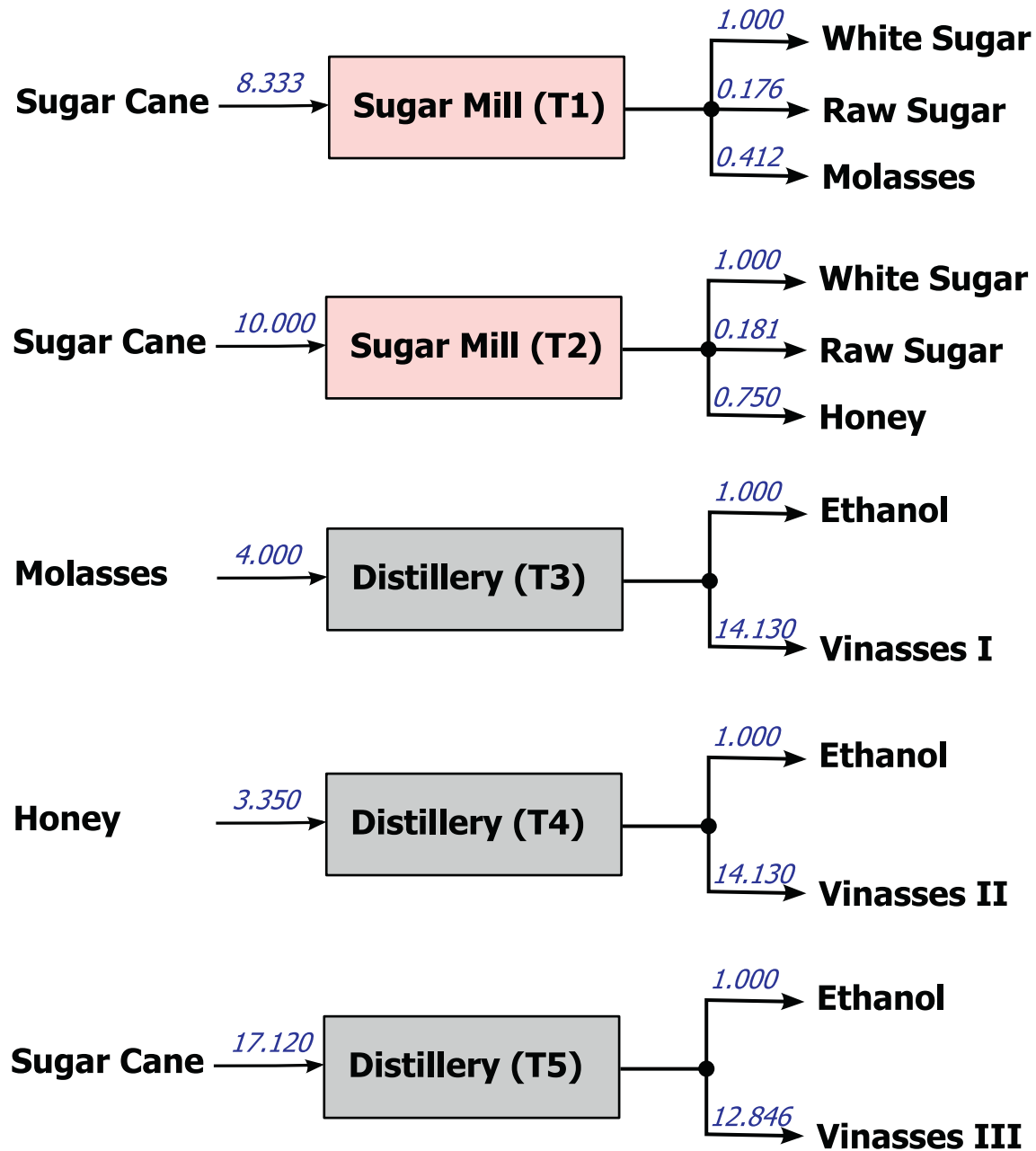


Fig. 2. Set of technologies. The labels T1, T2, ..., T5 indicate the technology used; the numbers above the arrows correspond to the mass balance coefficients.

distinguished by their sucrose content. Molasses is a viscous dark honey whose low sucrose content cannot be separated by crystallization, while secondary honey is a honey with a larger amount of sucrose that leaves the sugar mill before being exhausted by crystallization. Anhydrous ethanol can be produced by fermentation and following dehydration of different process streams: molasses (T3), honey (T4) and sugar cane juice (T5). According to this, the model considers five different technologies, two for sugar production and three types of distilleries. The details of each technology, including the mass balance coefficients, are shown in Fig. 2. We assume that bagasse is completely utilized for internal purposes, so the model includes a set of nine materials: sugar cane, ethanol, molasses, honey, white sugar, raw sugar, vinasse type 1, vinasse type 2 and vinasse type 3.

All the considered technologies require a water feed. For example, sugar mills T1 and T2 use water for the imbibition of the chopped sugar cane. In the technologies T3 and T4, molasses or

honey must be diluted before the fermentation step. Distillery T5 utilizes water for two purposes: extraction and dilution of sugar cane juice. We do not consider a water supply, but the cost of water is included in the parameter  $UPC_{ipgt}$  (unit production cost).

Each plant type incurs fixed capital and operating costs and may be expanded in capacity over time in order to follow a specific demand pattern. The establishment of a plant type is determined from the demand of the sub-region, the capacity that the sub-region has to fulfill its internal needs and the cost data.

#### Storage facilities

The model includes two different types of storage facilities: warehouses for liquid products and warehouses for solid materials. Each storage facility type has fixed capital and unit storage costs, and lower and upper limits for capacity expansions. The stor-



age capacity might be expanded in order to follow changes in the demand as well as in the supply.

We do not consider feed storage facilities in the supply chain. The reason for this is that the freshly cut sugar cane must be transported to the factory without any delay, because it loses its sugar content very rapidly. Moreover, damage to the cane during mechanical harvesting accelerates this decline. Hence, the sugar cane must be transported to a sugar mill within 24 hours after harvest at the latest (Shreve & Austin, 1984).

### Transportation modes

Transportation links allow to deliver final products to customers, supply the plants with raw materials and dispose the process wastes. The model assumes that the transportation tasks can be performed by three types of trucks: heavy trucks with open-box bed for sugar cane, lorries for sugar and tank trucks for liquid products. Each type of transportation mode has fixed capital and unit transportation costs and lower and upper limits for its capacity. The number and capacity of the transportation links can also vary over time in order to follow a given demand pattern.

### 3.1. General constraints

We next describe the main mathematical constraints of the model, which have been derived bearing in mind the particular features of the sugar cane industry in Argentina.

#### Materials balance

The starting point for all design is the material balance. Particularly, the law of conservation of mass must be satisfied in every sub-region. The overall mass balance for each sub-region is represented by Eq. (1). In accordance with it, for every material form  $i$ , the initial inventory kept in sub-region  $g$  from previous period ( $ST_{isgt-1}$ ) plus the amount produced ( $PT_{igt}$ ), the amount of raw materials purchased ( $PU_{igt}$ ) and the input flow rate from other facilities in the SC ( $Q_{ilg't}$ ) must equal the final inventory ( $ST_{isgt}$ ) plus the amount delivered to customers ( $DTS_{igt}$ ) plus the output flow to other sub-regions ( $Q_{ilgg't}$ ) and the amount of waste ( $W_{igt}$ ).

$$\sum_{i \in SI(i)} ST_{isgt-1} + PT_{igt} + PU_{igt} + \sum_{l \in LI(i)g' \neq g} Q_{ilg't} = \sum_{s \in SI(i)} ST_{isgt} + DTS_{igt} + \sum_{l \in LI(i)g' \neq g} Q_{ilgg't} + W_{igt} \quad \forall i, g, t \quad (1)$$

In this equation,  $SI(i)$  represents the set of technologies that can be used to store product  $i$ , whereas  $LI(i)$  are the set of transportation modes that can transport product  $i$ . Furthermore, the amount of products delivered to the final markets should be less than or equal to the actual demand ( $SD_{igt}$ ):

$$DTS_{igt} \leq SD_{igt} \quad \forall i, g, t \quad (2)$$

#### Production

The total production rate of material  $i$  in sub-region  $g$  is determined from the particular production rates ( $PE_{ipgt}$ ) of each technology  $p$  installed in the sub-region:

$$PT_{igt} = \sum_p PE_{ipgt} \quad \forall i, g, t \quad (3)$$

The details of each technology, including the mass balance coefficients, are shown in Fig. 2, where residuals, water feed, loses and discards are omitted. As observed, the material balance coefficients of the main products (white sugar and ethanol) have been normalized to 1. The production rates of byproducts and raw materials for

each technology are calculated from the material balance coefficients,  $\rho_{pi}$ , and the production rates of the main products:

$$PE_{ipgt} = \rho_{pi} PE_{ipgt} \quad \forall i, p, g, t, \quad \forall i' \in IM(p) \quad (4)$$

In this equation,  $IM(p)$  represents the set of main products associated with each technology. The values of the material balance coefficients are negative for feedstocks and positive for products/by-products. The production rate of each technology  $p$  in sub-region  $g$  is limited by the minimum desired percentage of the available technology that must be utilized,  $\tau$ , multiplied by the existing capacity (represented by the continuous variable  $PCap_{pgt}$ ) and the maximum capacity:

$$\tau PCap_{pgt} \leq PE_{ipgt} \leq PCap_{pgt} \quad \forall i, p, g, t \quad (5)$$

The capacity of technology  $p$  in any time period  $t$  is calculated adding the existing capacity at the end of the previous period to the expansion in capacity,  $PCapE_{pgt}$ , carried out in period  $t$ :

$$PCap_{pgt} = PCap_{pgt-1} + PCapE_{pgt} \quad \forall p, g, t \quad (6)$$

Eq. (7) bounds the capacity expansion  $PCapE_{pgt}$  between upper and lower limits, which are calculated from the number of plants installed in the sub-region ( $NP_{gpt}$ ) and the minimum and maximum capacities associated with each technology  $p$  ( $\underline{PCap}_p$  and  $\overline{PCap}_p$ , respectively).

$$\underline{PCap}_p NP_{gpt} \leq PCapE_{pgt} \leq \overline{PCap}_p NP_{gpt} \quad \forall p, g, t \quad (7)$$

The purchases of sugar cane are limited by the capacity of the existing sugar cane plantation in sub-region  $g$  and time interval  $t$ :

$$PU_{igt} \leq CapCrop_{gt} \quad \forall i = \text{sugar cane}, g, t \quad (8)$$

#### Storage

As occurs with plants, the storage capacity is limited by lower and upper bounds, which are given by the number of storage facilities installed in sub-region  $g$  ( $NS_{sgt}$ ) and the minimum and maximum storage capacities ( $\underline{SCap}_s$  and  $\overline{SCap}_s$ , respectively) associated with each storage technology:

$$\underline{SCap}_s NS_{sgt} \leq SCapE_{sgt} \leq \overline{SCap}_s NS_{sgt} \quad \forall s, g, t \quad (9)$$

The capacity of a storage technology  $s$  in any time period  $t$  is determined from the existing capacity at the end of the previous period and the expansion in capacity in the current period ( $SCapE_{sgt}$ ):

$$SCap_{sgt} = SCap_{sgt-1} + SCapE_{sgt} \quad \forall s, g, t \quad (10)$$

The storage capacity should be enough to store the total inventory ( $ST_{isgt}$ ) of product  $i$  during time interval  $t$ :

$$\sum_{i \in IS(s)} ST_{isgt} \leq SCap_{sgt} \quad \forall s, g, t \quad (11)$$

In this equation,  $IS(s)$  denotes the set of products that can be stored by technology  $s$ . During steady-state operation, the average inventory ( $AIL_{igt}$ ) is a function of the amount delivered to customers and the storage period  $\beta$ :

$$AIL_{igt} = \beta DTS_{igt} \quad \forall i, g, t \quad (12)$$

The storage capacity ( $SCap_{sgt}$ ) that should be established in a sub-region in order to cope with fluctuations in both supply and demand, is twice the average inventory levels of products  $i$  (Simchi-Levi, Kamisky, & Simchi-Levi, 2000).

$$2AIL_{igt} \leq \sum_{s \in SI(i)} SCap_{sgt} \quad \forall i, g, t \quad (13)$$

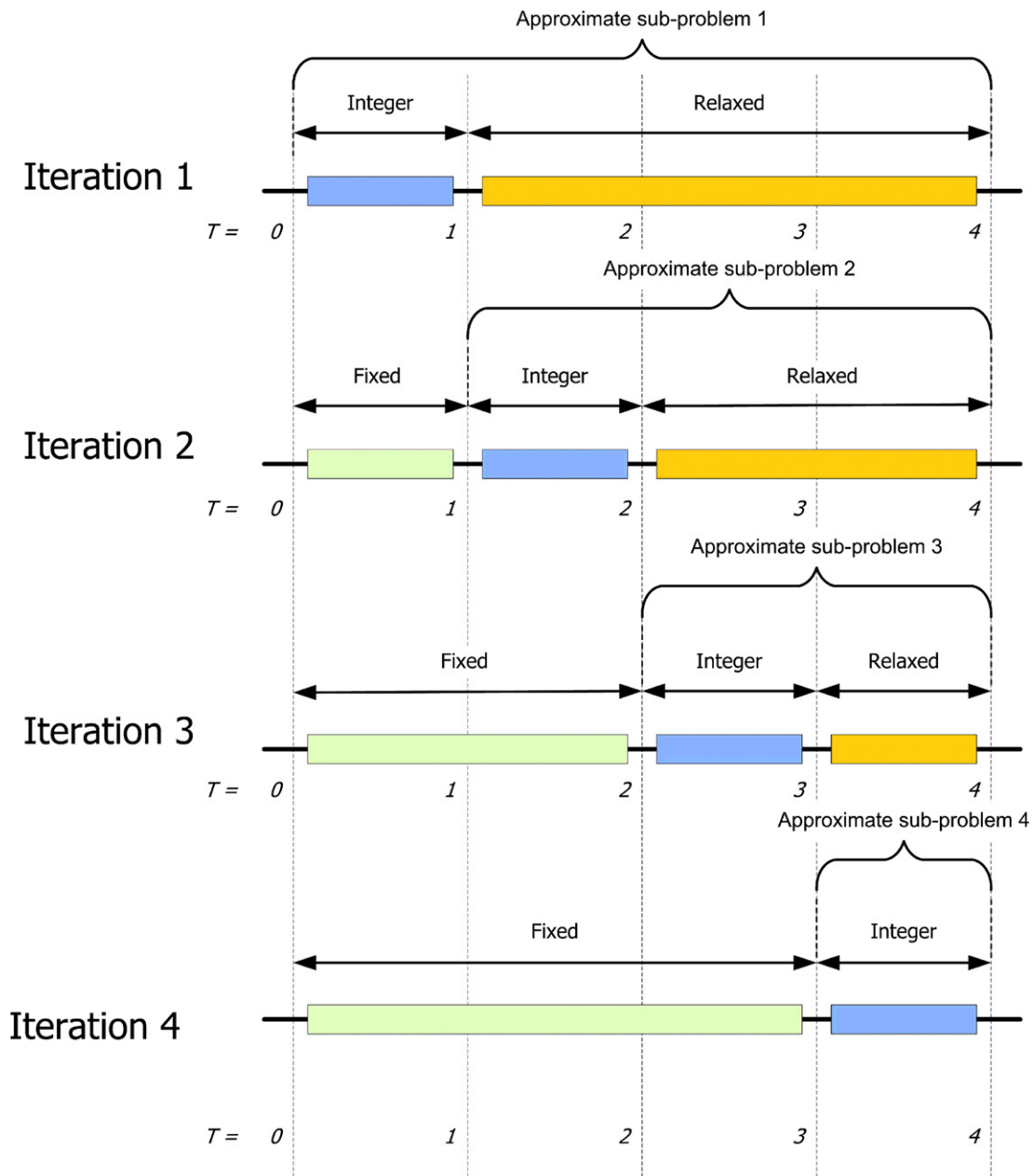


Fig. 3. Application of the “rolling horizon” strategy to a four-time-period problem.

#### Transportation

The existence of a transportation link between two sub-regions  $g$  and  $g'$  is represented by a binary variable  $X_{lgg't}$  which equals 1 if a transportation link is established between the two sub-regions and 0 otherwise. The definition of this variable is enforced via Eq. (14), which constraints the materials flow between minimum and maximum allowable capacity limits ( $\underline{Q}_l$  and  $\overline{Q}_l$ , respectively):

$$\underline{Q}_l X_{lgg't} \leq \sum_{i \in IL(l)} Q_{ilgg't} \leq \overline{Q}_l X_{lgg't} \quad \forall l, t, g, g' (g' \neq g) \quad (14)$$

In this equation,  $IL(l)$  represents the set of materials that can be transported via transportation mode  $l$ . Furthermore, a sub-region can either import or export material  $i$ , but not both at the same

time:

$$X_{lgg't} + X_{lg'gt} = 1 \quad \forall l, t, g, g' (g' \neq g) \quad (15)$$

#### 3.2. Objective function

The use of NPV as an objective function is a widely-spread approach in investment planning. In most cases it results in a linear model, which can be effectively solved by standard branch-and-bound methods. However, the NPV measure does not account appropriately for the rate at which the investment is recovered because it tends to add investment that has marginal or meaningless returns. Bagajewicz (2008) pointed out that additional procedures and measures are needed in planning problems. Particularly, the return of investment (ROI) is a more appropriate key performance indicator when there are other investment alterna-

**Table 1**  
Mean values for demand, ton/year.

| Name of province    | Associated sub-region | Product form |            |            |
|---------------------|-----------------------|--------------|------------|------------|
|                     |                       | White sugar  | Raw sugar  | Ethanol    |
| Buenos Aires        | G01                   | 76,614.92    | 38,307.46  | 84,276.41  |
| Córdoba             | G02                   | 84,126.19    | 42,063.09  | 92,538.81  |
| Corrientes          | G03                   | 25,438.16    | 12,719.08  | 27,981.97  |
| La Plata            | G04                   | 379,268.90   | 189,634.45 | 417,195.79 |
| La Rioja            | G05                   | 9714.57      | 4857.29    | 10,686.03  |
| Mendoza             | G06                   | 43,565.35    | 21,782.67  | 47,921.88  |
| Neuquén             | G07                   | 13,720.58    | 6860.29    | 15,092.64  |
| Entre Ríos          | G08                   | 31,547.32    | 15,773.66  | 34,702.05  |
| Misiones            | G09                   | 27,140.71    | 13,570.36  | 29,854.78  |
| Chubut              | G10                   | 11,517.28    | 5758.64    | 12,669.00  |
| Chaco               | G11                   | 26,439.66    | 13,219.83  | 29,083.63  |
| Santa Cruz          | G12                   | 5708.56      | 2854.28    | 6279.42    |
| Salta               | G13                   | 30,746.12    | 15,373.06  | 33,820.73  |
| San Juan            | G14                   | 17,526.29    | 8763.14    | 19,278.92  |
| San Luis            | G15                   | 11,016.52    | 5508.26    | 12,118.18  |
| Tucumán             | G16                   | 37,155.73    | 18,577.87  | 40,871.31  |
| Jujuy               | G17                   | 17,125.69    | 8562.84    | 18,838.26  |
| Santa Fe            | G18                   | 81,121.68    | 40,560.84  | 89,233.85  |
| La Pampa            | G19                   | 8412.62      | 4206.31    | 9253.88    |
| Santiago del Estero | G20                   | 21,732.60    | 10,866.30  | 23,905.86  |
| Catamarca           | G21                   | 8612.92      | 4306.46    | 9474.21    |
| Río Negro           | G22                   | 15,022.53    | 7511.27    | 16,524.79  |
| Formosa             | G23                   | 13,520.28    | 6760.14    | 14,872.31  |
| Tierra del Fuego    | G24                   | 3204.81      | 1602.40    | 3525.29    |

tives competing for the same capital. In the context of a SC design problem like the one addressed in this article, one way in which this metric can be evaluated is using the ratio between the average cash flows ( $CF_t$ ) and the fixed capital investment  $FCI$ :

$$ROI = \frac{\left( \sum_t CF_t \right) / T}{FCI} \quad (16)$$

As observed, the introduction of the  $ROI$  as the economic indicator to be maximized gives rise to a mixed-integer linear fractional programming formulation that can be solved using the Dinkelbach's algorithm. Given that the linear NPV-based approach already has computational issues that this paper attempts to ameliorate, following Bagajewicz (2008) we resort to solving a series of MILPs that maximize the NPV for different upper bounds on  $FCI$ . As discussed in Bagajewicz (2008), from these results one can identify solutions close to the maximum  $ROI$  one.

The NPV can be determined from the discounted cash flows generated in each of the time intervals  $t$  in which the total time horizon is divided:

$$NPV = \sum_t \frac{CF_t}{(1+ir)^{t-1}} \quad (17)$$

In this equation,  $ir$  represents the interest rate. The cash flow that appears in Eq. (17) in each time period is computed from the net earnings  $NE_t$  (i.e., profit after taxes), and the fraction of the total depreciable capital ( $FTDC_t$ ) that corresponds to that period as follows:

$$CF_t = NE_t - FTDC_t, \quad t = 1, \dots, T-1 \quad (18)$$

In the calculation of the cash flow of the last time period ( $t=T$ ), we assume that part of the total fixed capital investment may be recovered at the end of the time horizon. This amount, which represents the salvage value of the network ( $sv$ ), may vary from one type of industry to another.

$$CF_t = NE_t - FTDC_t + svFCI, \quad t = T \quad (19)$$

**Table 2**  
Distances between sub-regions, km.

|      |      |      |      |      |      |      |      |      |      |      |      |      |      |      |      |      |      |      |      |      |      |      |      |
|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|
| G01  | G02  | G03  | G04  | G05  | G06  | G07  | G08  | G09  | G10  | G11  | G12  | G13  | G14  | G15  | G16  | G17  | G18  | G19  | G20  | G21  | G22  | G23  | G24  |
| 0    | 711  | 933  | 60   | 1167 | 1080 | 1178 | 511  | 1008 | 1379 | 953  | 2542 | 1542 | 1140 | 800  | 1229 | 1565 | 484  | 607  | 1070 | 1122 | 948  | 1098 | 3162 |
| 711  | 0    | 900  | 768  | 460  | 680  | 1153 | 360  | 1118 | 1524 | 880  | 2638 | 844  | 600  | 420  | 597  | 867  | 340  | 667  | 439  | 433  | 1208 | 1031 | 3258 |
| 933  | 900  | 0    | 990  | 1024 | 1490 | 1913 | 573  | 335  | 2206 | 20   | 3369 | 830  | 1460 | 1190 | 794  | 853  | 540  | 1388 | 635  | 857  | 1774 | 186  | 3989 |
| 60   | 768  | 990  | 0    | 1224 | 1137 | 1159 | 568  | 1065 | 1371 | 1010 | 2533 | 1599 | 1197 | 857  | 1286 | 1622 | 541  | 664  | 1127 | 1173 | 924  | 1236 | 3153 |
| 1167 | 460  | 1024 | 1224 | 0    | 612  | 1427 | 820  | 1333 | 1872 | 1007 | 3087 | 704  | 355  | 559  | 382  | 727  | 800  | 1015 | 389  | 171  | 1565 | 1139 | 3707 |
| 1080 | 680  | 900  | 768  | 1427 | 0    | 815  | 952  | 1710 | 1628 | 1470 | 2783 | 1311 | 166  | 264  | 872  | 1329 | 930  | 789  | 1007 | 725  | 1342 | 1600 | 3403 |
| 1178 | 1153 | 1913 | 1159 | 1427 | 815  | 0    | 1413 | 2075 | 746  | 1880 | 1909 | 1997 | 981  | 890  | 1581 | 2020 | 1373 | 535  | 1618 | 1536 | 557  | 2020 | 2529 |
| 511  | 360  | 573  | 568  | 820  | 952  | 1413 | 0    | 758  | 1715 | 590  | 2887 | 1107 | 950  | 691  | 794  | 1130 | 30   | 855  | 635  | 803  | 1252 | 746  | 3507 |
| 1008 | 1118 | 335  | 1065 | 1333 | 1710 | 2075 | 758  | 0    | 2356 | 332  | 3511 | 1142 | 1708 | 1449 | 1086 | 1165 | 785  | 1518 | 927  | 1179 | 1896 | 508  | 4131 |
| 1379 | 1524 | 2206 | 1371 | 1872 | 1628 | 746  | 1715 | 2356 | 0    | 2236 | 1172 | 2308 | 1705 | 1382 | 2107 | 2331 | 1685 | 857  | 1986 | 1900 | 809  | 2450 | 1792 |
| 953  | 880  | 20   | 1010 | 1007 | 1470 | 1880 | 590  | 332  | 2236 | 0    | 3388 | 813  | 1460 | 1190 | 774  | 833  | 540  | 1368 | 618  | 820  | 1756 | 173  | 4008 |
| 2542 | 2638 | 3369 | 2533 | 3087 | 2783 | 1909 | 2887 | 3511 | 1172 | 3388 | 0    | 3482 | 2868 | 2545 | 3192 | 3505 | 2850 | 2020 | 3070 | 1617 | 3593 | 620  | 959  |
| 1542 | 844  | 830  | 60   | 460  | 680  | 1153 | 360  | 1118 | 1524 | 880  | 2638 | 0    | 1150 | 420  | 597  | 867  | 920  | 1462 | 472  | 533  | 2066 | 959  | 4102 |
| 1140 | 600  | 900  | 768  | 1167 | 1080 | 1178 | 511  | 1008 | 1379 | 953  | 2542 | 1542 | 0    | 320  | 708  | 1163 | 484  | 607  | 840  | 497  | 1509 | 1540 | 3488 |
| 800  | 420  | 1190 | 794  | 1224 | 597  | 867  | 340  | 667  | 439  | 433  | 1208 | 1031 | 3258 | 0    | 838  | 1287 | 340  | 667  | 840  | 497  | 1509 | 1540 | 3488 |
| 1229 | 948  | 1098 | 3162 | 3707 | 3403 | 2529 | 3507 | 4131 | 1792 | 4008 | 620  | 4102 | 3488 | 3165 | 3812 | 4125 | 3470 | 2640 | 3690 | 3787 | 2572 | 4213 | 0    |



**Table 3**  
Sugar cane capacity, ton/year.

| Province | Capacity   |
|----------|------------|
| Tucumán  | 12,220,000 |
| Jujuy    | 4,324,000  |
| Salta    | 2,068,000  |
| Santa Fe | 125,960    |
| Misiones | 62,040     |

**Table 4**  
Minimum and maximum production capacities of each technology (ton of main product per year).

|                             | Technologies |         |         |         |         |
|-----------------------------|--------------|---------|---------|---------|---------|
|                             | T1           | T2      | T3      | T4      | T5      |
| Minimum production capacity | 30,000       | 30,000  | 10,000  | 10,000  | 10,000  |
| Maximum production capacity | 350,000      | 350,000 | 300,000 | 300,000 | 300,000 |

**Table 5**  
Parameters used to evaluate the capital cost for different production technologies.

|    | $\alpha_{pgt}^{Pl}$ , \$ | $\beta_{pgt}^{Pl}$ , \$ year/ton |
|----|--------------------------|----------------------------------|
| T1 | 5,350,000                | 535                              |
| T2 | 5,350,000                | 535                              |
| T3 | 7,710,000                | 771                              |
| T4 | 7,710,000                | 771                              |
| T5 | 9,070,000                | 907                              |

**Table 6**  
Parameters used to evaluate the capital cost for different storage technologies.

|    | $\alpha_{sgt}^S$ , \$ | $\beta_{sgt}^S$ , \$ year/ton |
|----|-----------------------|-------------------------------|
| S1 | 1,220,000             | 122                           |
| S2 | 18,940,000            | 1894                          |

The net earnings are given by the difference between the incomes ( $Rev_t$ ) and the facility operating ( $FOC_t$ ), and transportation cost ( $TOC_t$ ), as it is stated in Eq. (20):

$$NE_t = (1 - \varphi)(Rev_t - FOC_t - TOC_t) + \varphi DEP_t \quad \forall t \quad (20)$$

In this equation,  $\varphi$  denotes the tax rate. The revenues are determined from the sales of final products and the corresponding prices

**Table 7**  
Prices of final products.

|                          | Price, \$/ton |
|--------------------------|---------------|
| White sugar <sup>a</sup> | 734           |
| Raw sugar <sup>b</sup>   | 615           |
| Ethanol <sup>c</sup>     | 598           |

<sup>a</sup> No. 407 LIFFE white sugar futures contract

<sup>b</sup> No. 11 ICE raw sugar futures contract

<sup>c</sup> QE NYMEX ethanol futures contract

**Table 8**  
Parameters used to calculate the capital and operating cost for different transportation modes.

|   | Heavy truck | Lorry  | Tanker truck |
|---|-------------|--------|--------------|
| Average speed (km/h)                          | 55          | 60     | 60           |
| Capacity (ton/trip)                           | 30          | 25     | 20           |
| Availability of transportation mode (h/day)   | 18          | 18     | 18           |
| Cost of establishing transportation mode (\$) | 90,000      | 65,000 | 100,000      |
| Driver wage (\$/h)                            | 10          | 10     | 10           |
| Fuel economy (km/L)                           | 5           | 5      | 5            |
| Fuel price (\$/L)                             | 0.85        | 0.85   | 0.85         |
| General expenses (\$/day)                     | 8.22        | 8.22   | 8.22         |
| Load/unload time of product (h/trip)          | 6           | 6      | 6            |
| Maintenance expenses (\$/km)                  | 0.0976      | 0.0976 | 0.0976       |

( $PR_{igt}$ ):

$$Rev_t = \sum_{i \in SEP} \sum_g DTS_{igt} PR_{igt} \quad \forall t \quad (21)$$

In this equation  $SEP$  represents the set of materials  $i$  that can be sold. The facility operating cost is obtained by multiplying the unit production and storage costs ( $UPC_{ipgt}$  and  $USC_{isgt}$ , respectively) by the corresponding production rates and average inventory levels, respectively. This term includes also the disposal cost ( $DC_t$ ):

$$FOC_t = \sum_i \sum_g \sum_{i \in IM(p)} UPC_{ipgt} PE_{ipgt} + \sum_i \sum_g \sum_{i \in IS(s)} USC_{isgt} AIL_{igt} + DC_t \quad \forall t \quad (22)$$

**Table 9**  
Comparison of “full space” method and “rolling horizon” approach.

| Case | “Full space” solution      | CPU <sup>a</sup> | “Rolling horizon” approach |       |        |                   |       |        |                 |     |        |
|------|----------------------------|------------------|----------------------------|-------|--------|-------------------|-------|--------|-----------------|-----|--------|
|      |                            |                  | 0% <sup>b</sup>            | CPU   | Error  | 0.5% <sup>c</sup> | CPU   | Error  | 1% <sup>d</sup> | CPU | Error  |
| 2    | 364,855,004                | 249              | 355,681,928                | 165   | 2.514% | 355,681,928       | 159   | 2.514% | 355,681,928     | 133 | 2.514% |
| 3    | 748,077,521                | 190              | 737,299,005                | 137   | 1.441% | 747,059,134       | 110   | 0.136% | 747,059,134     | 71  | 0.136% |
| 4    | 1,103,078,130              | 387              | 1,102,408,378              | 420   | 0.061% | 1,100,709,014     | 254   | 0.215% | 1,072,612,733   | 122 | 2.762% |
| 5    | 1,488,103,667              | 975              | 1,481,385,696              | 428   | 0.451% | 1,473,161,834     | 285   | 1.004% | 1,481,093,288   | 56  | 0.471% |
| 6    | 1,800,100,718              | 4,915            | 1,793,499,301              | 880   | 0.367% | 1,794,272,262     | 378   | 0.324% | 1,792,417,632   | 110 | 0.427% |
| 7    | 2,073,908,387              | 14,468           | 2,065,178,757              | 1996  | 0.421% | 2,066,786,891     | 687   | 0.343% | 2,071,299,494   | 128 | 0.126% |
| 8    | 2,382,730,430              | 27,608           | 2,372,869,869              | 2548  | 0.414% | 2,373,873,363     | 702   | 0.372% | 2,370,793,357   | 345 | 0.501% |
| 9    | 2,599,013,033 <sup>e</sup> | 43,200           | 2,591,023,707              | 7,140 | 0.487% | 2,574,336,476     | 1,928 | 1.128% | 2,592,387,982   | 455 | 0.435% |
| 10   | 2,790,699,079 <sup>e</sup> | 43,200           | 2,791,675,712              | 3,637 | 0.356% | 2,785,727,849     | 2,415 | 0.569% | 2,756,152,808   | 308 | 1.624% |

<sup>a</sup> CPU time in seconds.

<sup>b</sup> Solution calculated by the “rolling-horizon” method solving the sub-problems with 0% of optimality gap.

<sup>c</sup> Solution calculated by the “rolling-horizon” method solving the sub-problems with 0.5% of optimality gap.

<sup>d</sup> Solution calculated by the “rolling-horizon” method solving the sub-problems with 1% of optimality gap.

<sup>e</sup> Best integer solution after 12 h.

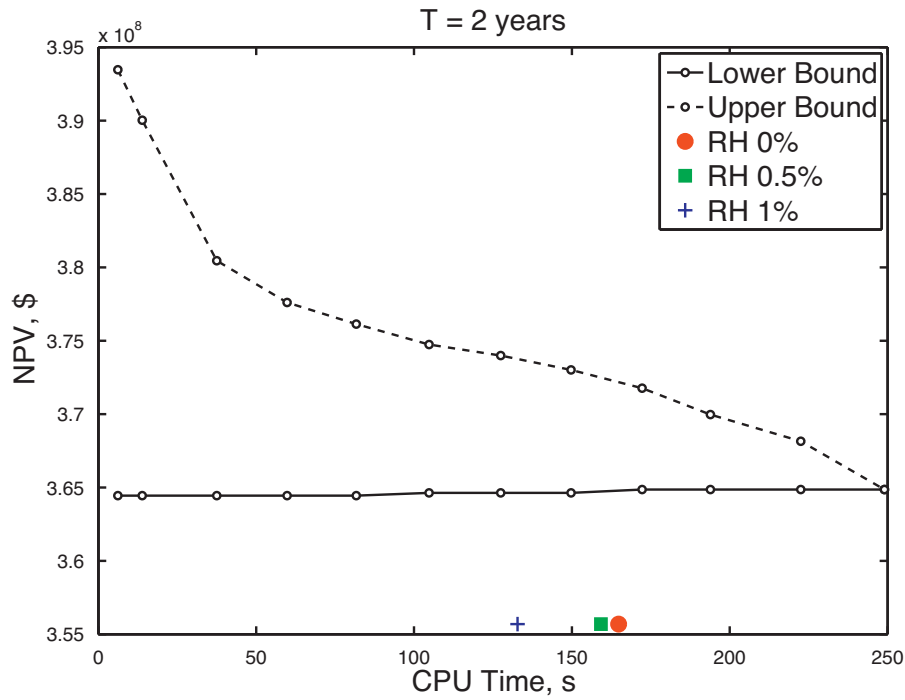


Fig. 4. Comparison of “full space” method vs. “rolling horizon” algorithm (for different optimality gaps imposed on the sub-problems) applied to a two-time-period problem.

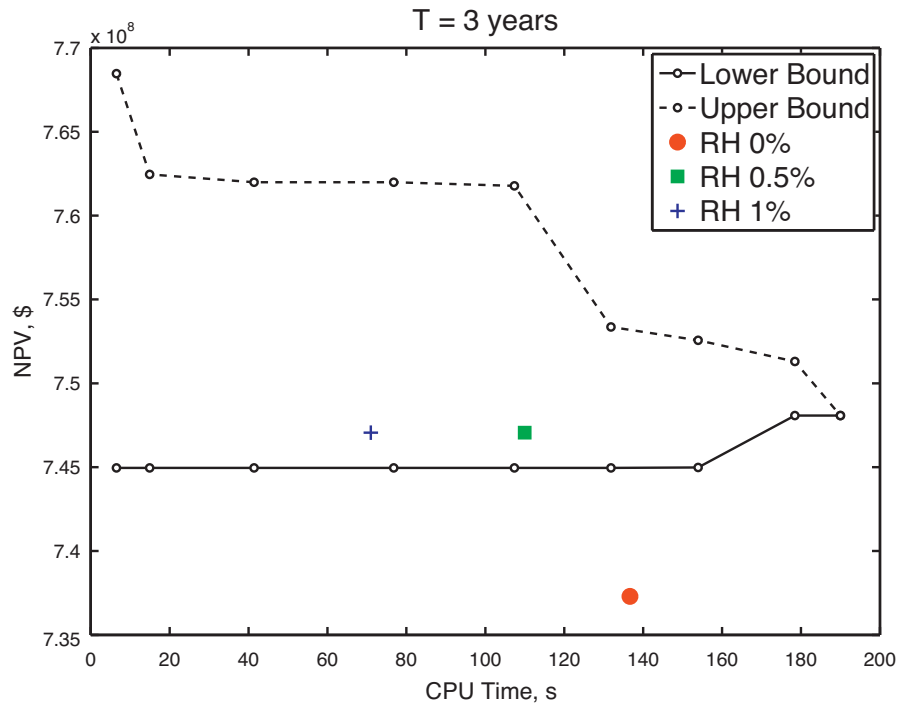


Fig. 5. Comparison of “full space” method vs. “rolling horizon” algorithm (for different optimality gaps imposed on the sub-problems) applied to a three-time-period problem.

The disposal cost is a function of the amount of waste and landfill tax ( $LT_{ig}$ ):

$$DC_t = \sum_i \sum_g W_{igt} LT_{ig} \quad \forall t \quad (23)$$

The transportation cost includes the fuel ( $FC_t$ ), labour ( $LC_t$ ), maintenance ( $MC_t$ ) and general ( $GC_t$ ) costs:

$$TOC_t = FC_t + LC_t + MC_t + GC_t \quad \forall t \quad (24)$$

The fuel cost is a function of the fuel price ( $FP_{lt}$ ) and fuel usage:

$$FC_t = \sum_g \sum_{g' \neq g} \sum_l \sum_{i \in IL(l)} \left[ \frac{2EL_{gg'} Q_{ilgg't}}{FE_l TC_{ap_l}} \right] FP_{lt} \quad \forall t \quad (25)$$

In Eq. (25), the fractional term represents the fuel usage, and is determined from the total distance traveled in a trip ( $2EL_{gg'}$ ), the fuel consumption of transport mode  $l$  ( $FE_l$ ) and the number of trips made per period of time ( $Q_{ilgg't}/TC_{ap_l}$ ). Note that this equation

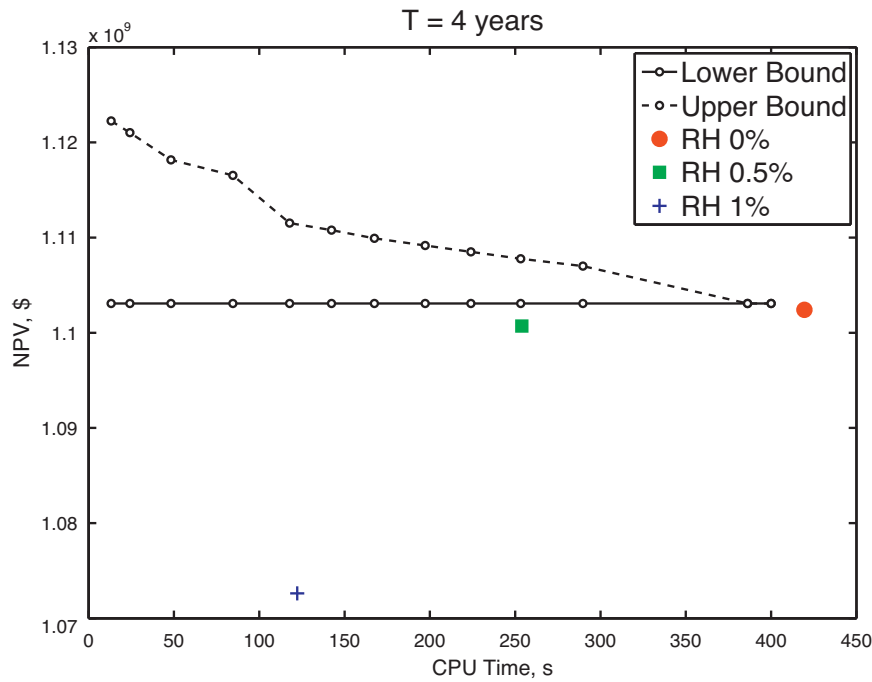


Fig. 6. Comparison of “full space” method vs. “rolling horizon” algorithm (for different optimality gaps imposed on the sub-problems) applied to a four-time-period problem.

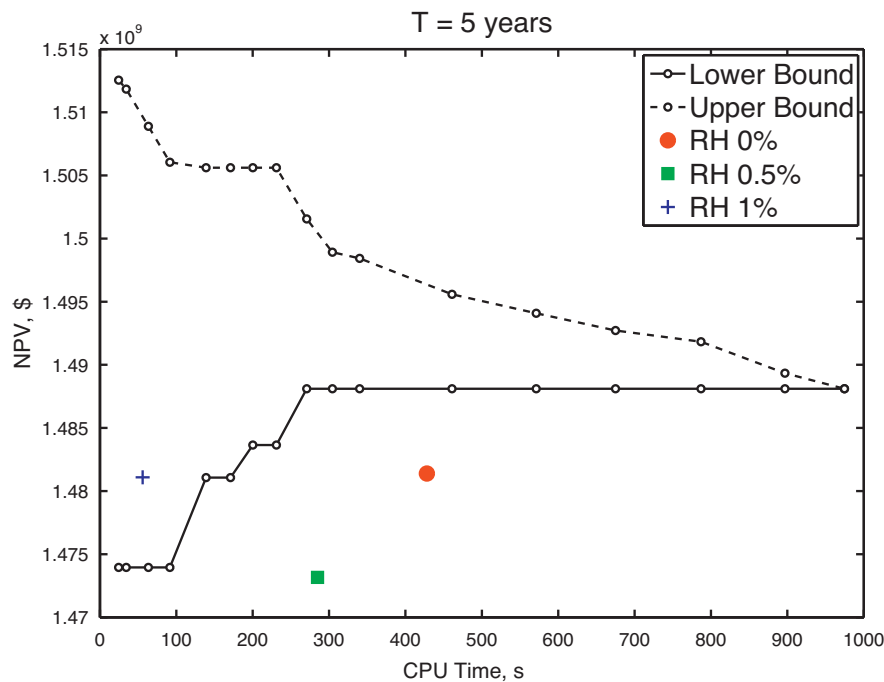


Fig. 7. Comparison of “full space” method vs. “rolling horizon” algorithm (for different optimality gaps imposed on the sub-problems) applied to a five-time-period problem.

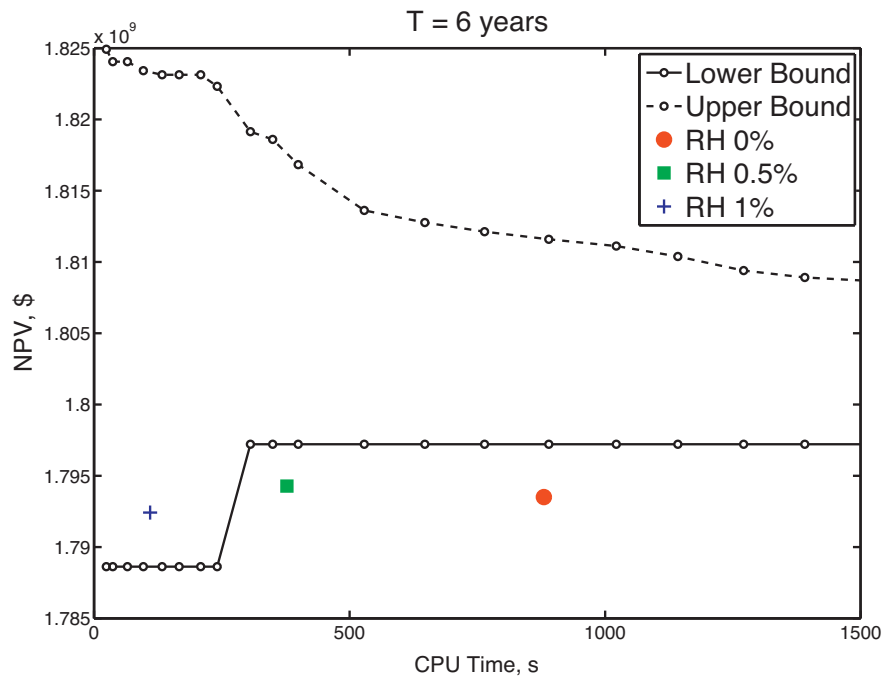
assumes that the transportation units operate only between two predefined sub-regions. Furthermore, as shown in Eq. (26), the labor transportation cost is a function of the driver wage ( $DW_{lt}$ ) and total delivery time (term inside the brackets):

$$LC_t = \sum_g \sum_{g' \neq g} \sum_l DW_{lt} \sum_{i \in IL(l)} \left[ \frac{Q_{ilgg't}}{TCap_l} \left( \frac{2EL_{gg'}}{SP_l} + LUT_l \right) \right] \quad \forall t \quad (26)$$

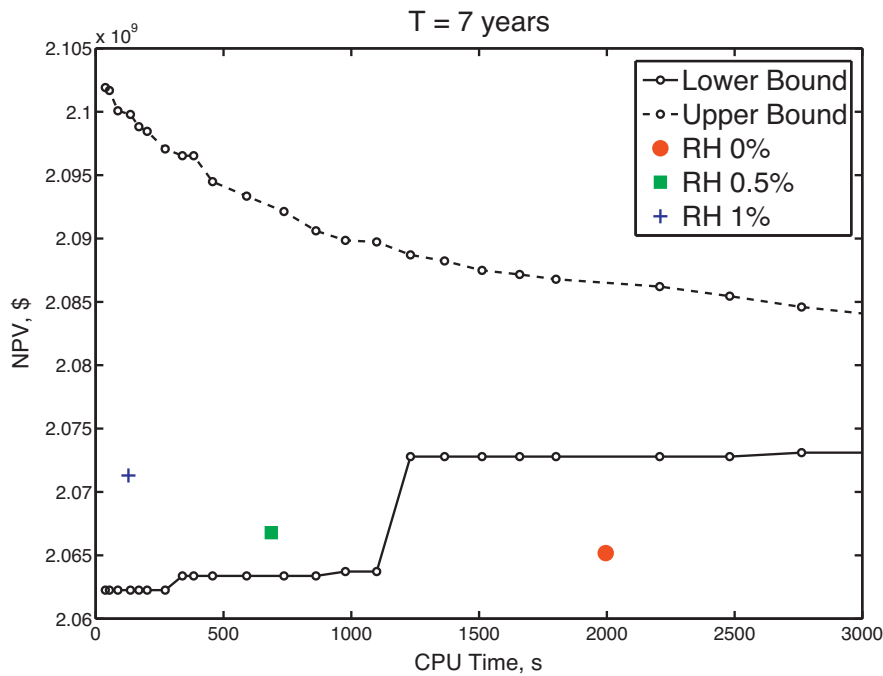
The maintenance cost accounts for the general maintenance of the transportation systems and is a function of the cost per unit of distance traveled ( $ME_l$ ) and total distance driven:

$$MC_t = \sum_g \sum_{g' \neq g} \sum_l \sum_{i \in IL(l)} ME_l \frac{2EL_{gg'} Q_{ilgg't}}{TCap_l} \quad \forall t \quad (27)$$

Finally, the general cost includes the transportation insurance, license and registration, and outstanding finances. It can be deter-



**Fig. 8.** Comparison of “full space” method vs. “rolling horizon” algorithm (for different optimality gaps imposed on the sub-problems) applied to a six-time-period problem.



**Fig. 9.** Comparison of “full space” method vs. “rolling horizon” algorithm (for different optimality gaps imposed on the sub-problems) applied to a seven-time-period problem.

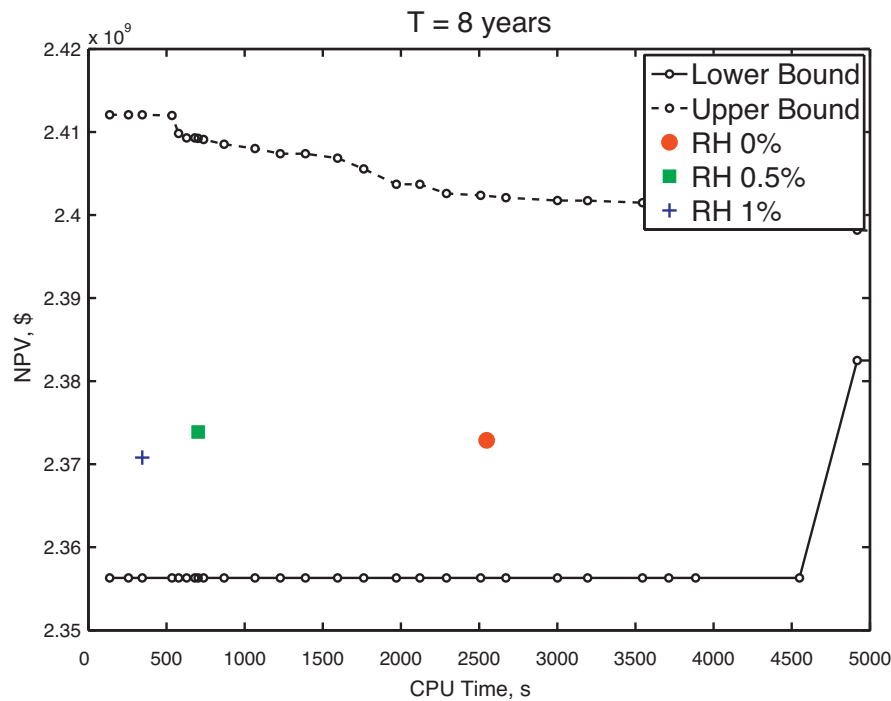
mined from the unit general expenses ( $GE_{lt}$ ) and number of transportation units ( $NT_{lt}$ ), as follows:

$$GC_t = \sum_l \sum_{t' \leq t} GE_{lt'} NT_{lt'} \quad \forall t \quad (28)$$

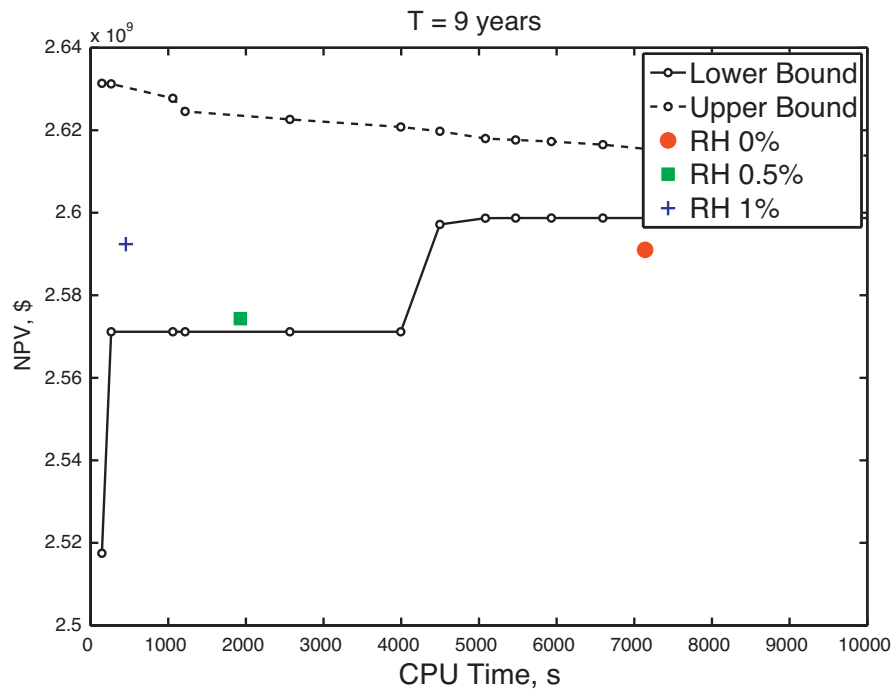
The depreciation term is calculated with the straight-line method:

$$DEP_t = \frac{(1 - sv)FCI}{T} \quad \forall t \quad (29)$$

where  $FCI$  denotes the total fixed cost investment, which is determined from the capacity expansions made in plants and warehouses as well as the purchases of transportation units during the



**Fig. 10.** Comparison of “full space” method vs. “rolling horizon” algorithm (for different optimality gaps imposed on the sub-problems) applied to an eight-time-period problem.



**Fig. 11.** Comparison of “full space” method vs. “rolling horizon” algorithm (for different optimality gaps imposed on the sub-problems) applied to a nine-time-period problem.

entire time horizon as follows:

$$\begin{aligned}
 FCI = & \sum_p \sum_g \sum_t (\alpha_{pgt}^{PL} NP_{pgt} + \beta_{pgt}^{PL} PCapE_{pgt}) \\
 & + \sum_s \sum_g \sum_t (\alpha_{sgt}^S NS_{sgt} + \beta_{sgt}^S SCapE_{sgt}) \\
 & + \sum_l \sum_t (NT_{lt} TMC_{lt})
 \end{aligned} \quad (30)$$

Here, the parameters  $\alpha_{pgt}^{PL}$ ,  $\beta_{pgt}^{PL}$  and  $\alpha_{sgt}^S$ ,  $\beta_{sgt}^S$  are the fixed and variable investment terms corresponding to plants and warehouses, respectively. On the other hand,  $TMC_{lt}$  is the investment cost associated with transportation mode  $l$ . The average number of trucks required to satisfy a certain flow between different sub-regions is computed from the flow rate of products between the sub-regions, the transportation mode availability ( $avl_l$ ), the capacity of a transport container, the average distance traveled between the sub-regions, the average speed, and the loading/unloading time, as



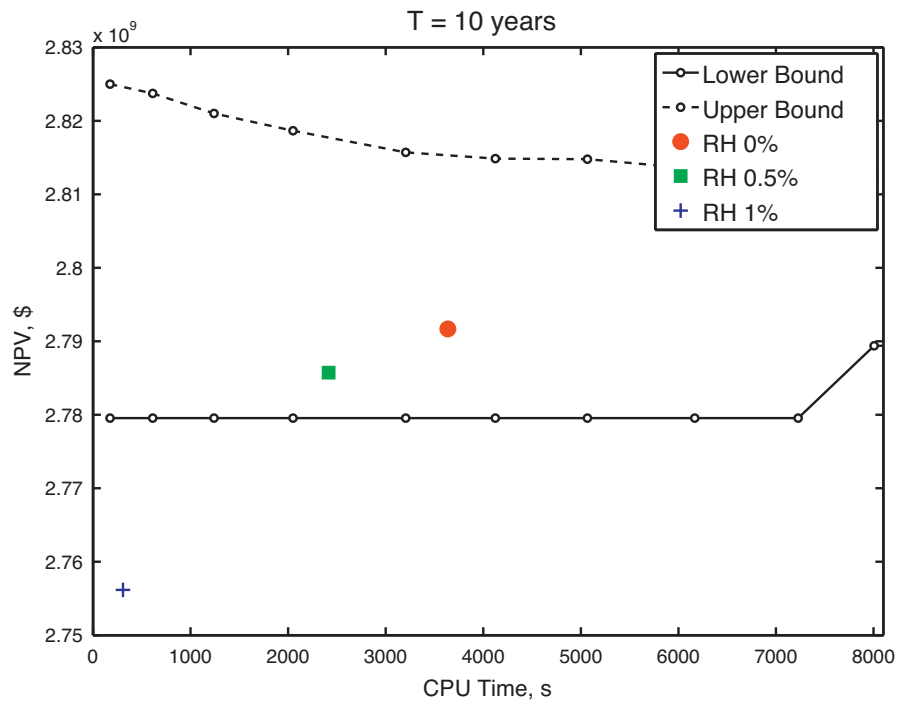


Fig. 12. Comparison of "full space" method vs. "rolling horizon" algorithm (for different optimality gaps imposed on the sub-problems) applied to a ten-time-period problem.

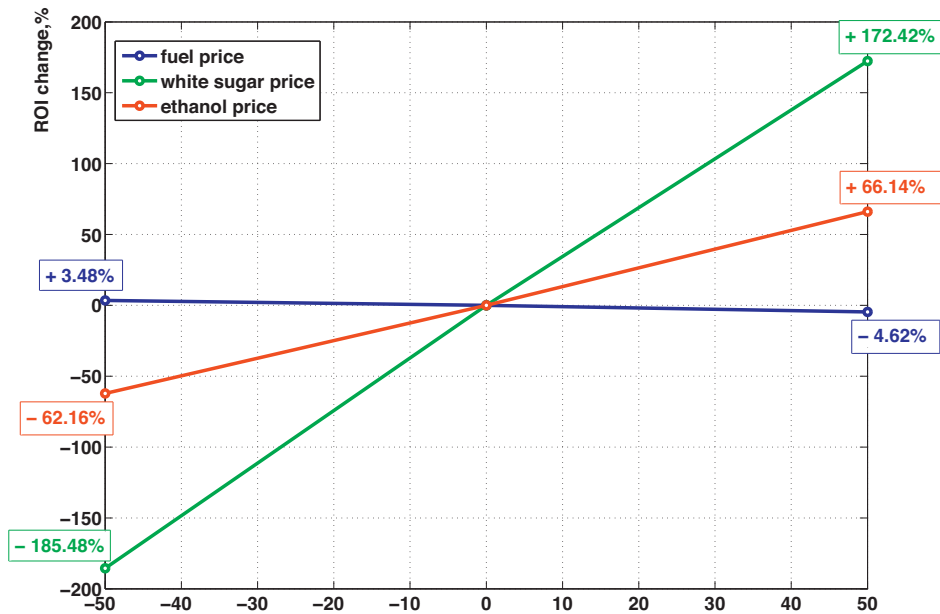


Fig. 13. Influence of fuel, sugar and ethanol prices on ROI.

stated in Eq. (31):

$$\sum_{t \leq T} NT_{lt} \geq \sum_{i \in IL(l)} \sum_g \sum_{g' \neq g} \sum_t \frac{Q_{ilgg't}}{avl_i TCap_l} \left( \frac{2EL_{gg'}}{SP_l} + LUT_l \right) \quad \forall l \quad (31)$$

The total amount of capital investment can be constrained to be lower than an upper limit, as stated in Eq. (32):

$$FCI \leq \overline{FCI} \quad (32)$$

Finally, the model assumes that the depreciation is linear over the time horizon. Thus, the depreciation term ( $FTDC_t$ ) is calculated as follows:

$$FTDC_t = \frac{FCI}{T} \quad \forall t \quad (33)$$

Finally, the overall MILP formulation is stated in compact form as follows:

$$\begin{aligned} & \max_{x, X, N} NPV(x, X, N) \quad (P) \\ & \text{s.t. constraints 1–33} \\ & x \in \mathbb{R}, \quad X \in \{0, 1\}, \quad N \in \mathbb{Z}^+ \end{aligned}$$

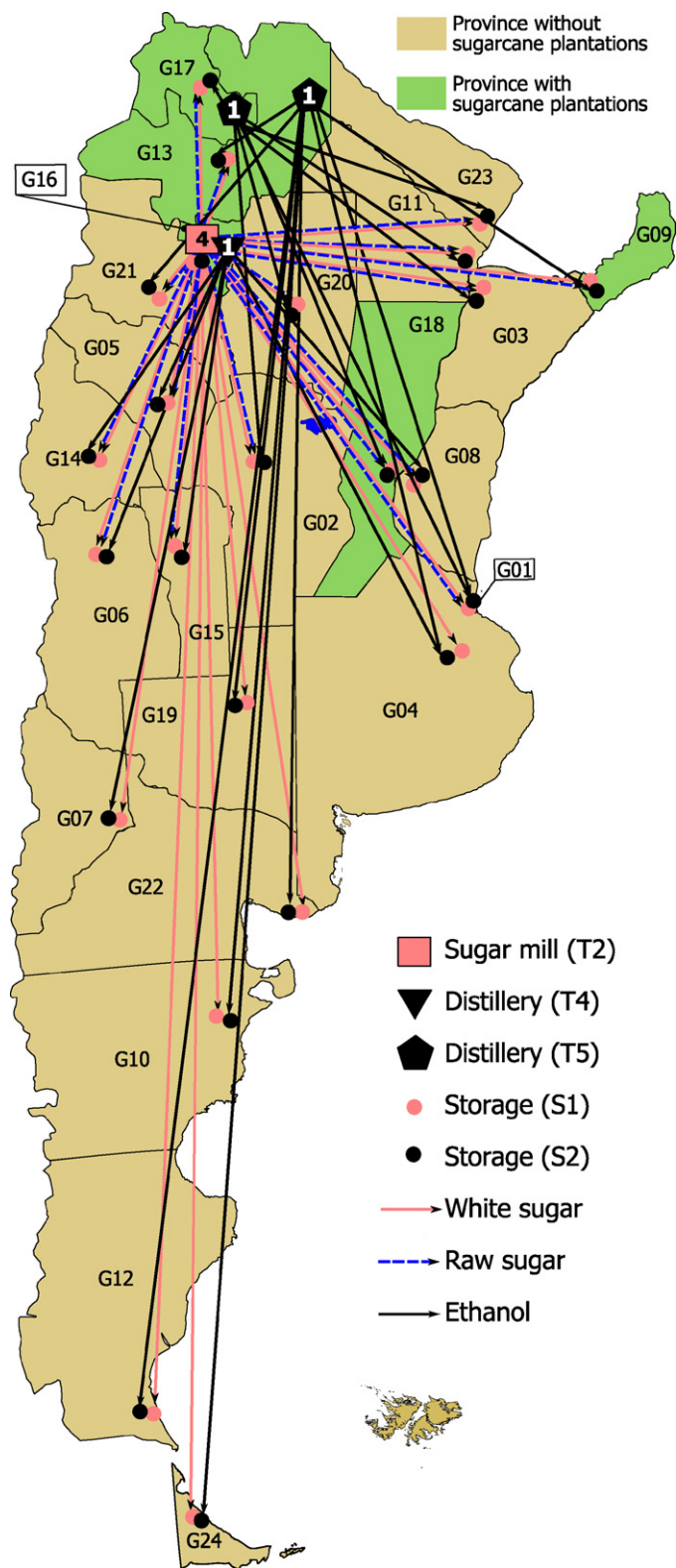


Fig. 14. Configuration of SC under base level of prices, high level of sugar price, low level of ethanol price, and all levels of fuel price.

Here,  $x$  denotes the continuous variables of the problem (capacity expansions, production rates, inventory levels and materials flows),  $X$  represents the binary variables (i.e., establishment of transportation links), and  $N$  is the set of integer variables denoting the number of plants, storage facilities and transportation units of each type selected.

The section that follows describes how the MILP problem described above can be efficiently solved via a customized rolling horizon algorithm, thus expediting the overall search for SC configurations that yield large ROI values.

#### 4. Solution approach

As shown in the previous section, the MILP model includes decision variables of different nature. The variables which represent the number of production and storage facilities to be installed ( $NP_{gpt}$  and  $NS_{sgt}$ , respectively) and number of transport modes purchased ( $NT_{it}$ ) are integer. Variables  $X_{lgt}$  denoting the existence of transportation links between sub-regions are binary, whereas the remaining variables are continuous. The overall MILP formulation can be solved via branch-and-bound techniques. The complexity of this MILP is mainly given by the number of integer and binary variables, which in our case increases with the number of time periods and sub-regions. Large-scale problems can therefore lead to branch-and-bound trees with a prohibitive number of nodes thus making the MILP computationally intractable. A decomposition method is presented next to reduce the computation burden of the model and facilitate the solution of problems of large size that might be found in practice.

The approach presented is based on a “rolling horizon” scheme (Balasubramanian & Grossmann, 2004; Dimitriadis et al., 1997; Elkamel & Mohindra, 1999), and consists of decomposing the original problem (P) into a number of smaller sub-problems that are solved in a sequential way. A typical “rolling horizon” algorithm relies on an approximate model (i.e., simplification of the original problem) that is formulated for the entire horizon of  $T$  time periods. In the first iteration, this model is solved providing decisions for the entire horizon, but only those belonging to the first time period are implemented. In the next iteration, the state of the system is updated, and another approximate model is solved for the remaining  $T-1$  time periods, freezing the decisions of the first time period already solved. The algorithm proceeds in this manner until all the decisions of the entire time horizon are calculated.

The traditional “rolling horizon” approach relies on solving a sequence of sub-problems of fixed length. This method is not directly applicable to our problem, mainly because there are constraints in our model that impose conditions that must be satisfied over the entire time horizon. Furthermore, the NPV calculation requires information from different time periods, which makes it difficult to implement the traditional “rolling horizon” approach.

Particularly, to derive the approximate models used by our “rolling horizon” strategy, we exploit the fact that the relaxation of the integer variables of the full space formulation (P) is very tight. In other words, the solution that is obtained when (P) is solved defining  $NP$ ,  $NS$ , and  $NT$  as continuous variables rather than as integers, is very close to the optimal solution of the original problem. The reason for this is that in practice these integer variables take large values, since they represent the number of facilities to be established in big regions that cover high demands.

Hence, the approximate models of our algorithm are constructed by relaxing the integer variables denoting the number of transportation units and production and storage facilities established in periods beyond the first one. The motivation behind this

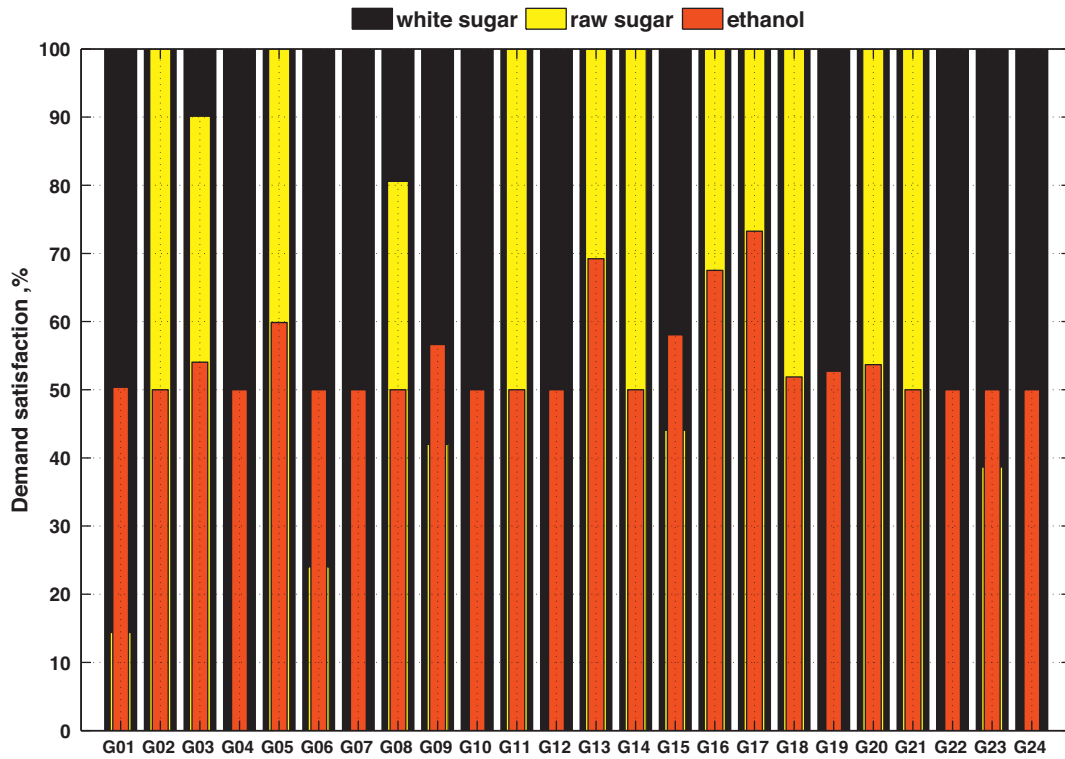


Fig. 15. Demand satisfaction level under base level of prices and high level of sugar prices.

procedure is that the computational complexity is greatly reduced by dropping the integrality requirement on these variables without sacrificing too much the quality of the solution. Therefore, in each iteration the method concentrates on determining the values of the integer variables of one single period, whereas the relaxed part of the problem allows to assess in an approximate manner the effect that these decisions have on later periods. The solutions of these sub-problems, all of which are relaxations of the original full space model (P), are then used to approximate the optimal solution of (P). Each sub-problem (AP) can therefore be expressed as follows:

$$\begin{aligned}
 &\max_{x, X, N} NPV(x, X, N) && \text{(AP)} \\
 &\text{s.t. constraints 1–33} \\
 &N = (N' \cup RN) \\
 &x \in \mathbb{R}, \quad RN \in \mathbb{R}, \quad X \in \{0, 1\}, \quad N' \in \mathbb{Z}^+
 \end{aligned}$$

where  $N' = (NP_{pgt'}, NS_{sgt'}, NT_{lt'})$  denotes the vector of integer variables corresponding to time period  $t'$  and  $RN = (RNP_{pgt}, RNS_{sgt}, RNT_{lt})$  is the vector of continuous variables representing the strategic decisions associated with those time intervals beyond  $t'$  (i.e.  $t > t'$ ). The “rolling horizon” algorithm proposed in this work is as follows:

### 1. Initialization.

Set iteration counter ( $ctr$ ) equal to 1.  
Go to step 2.

### 2. Solution.

Solve the subproblem (AP) with the branch-and-bound method relaxing the variables corresponding to those periods beyond  $ctr$ .  
Fix the variables for time interval  $t = ctr$ .

### 3. Termination check.

If  $ctr < T$ , then set  $ctr = ctr + 1$  and go to step 2.

Otherwise, there are no more sub-problems to be solved (termination).

Fig. 3 illustrates the way in which the algorithm would proceed for a problem with 4 time periods. Note that the time horizon of each approximate sub-problem is divided into two time blocks:

1. The “integer block”, which covers the first period of the sub-problem and in which all the integer decision variables  $NP_{pgt}$ ,  $NS_{sgt}$  and  $NT_{lt}$  remain unchanged. Note that this first interval moves forward as iterations proceed.
2. The “relaxed block”, which comprises all the periods beyond the current one, in which the integer variables denoting the number of production plants, storage facilities and transportation units are relaxed into continuous variables  $RNP_{pgt}$ ,  $RNS_{sgt}$  and  $RNT_{lt}$ , respectively.

### Remarks

- Before implementing the decomposition strategy, it is convenient to check the tightness of the integer relaxation of the model for small instances of the problem. If the relaxation is not tight enough, the method is not likely to work properly. In this case, alternative methods can be used (see Guillén-Gosálbez et al., 2010).
- The sub-problems can be constructed by relaxing only some of the integer variables instead of all of them. To choose the variables to be relaxed, one can perform a preliminary analysis in order to assess the impact of relaxing the variable on the CPU time and quality of the relaxation.

- The complexity of the model grows with the number of time periods, sub-regions and technologies. By merging neighboring sub-regions with low and high demands one can reduce the overall complexity of the model.
- It is not necessary to solve the sub-problems of the rolling-horizon method to global optimality. In fact, the overall method can be expedited by solving the sub-problems (AP) for low optimality gaps (i.e., less than 5%). This reduction in CPU time might be achieved at the expense of compromising the quality of the final solution.

## 5. Case study

In order to illustrate the capabilities and advantages of the proposed approach, a case study based on the sugar cane industry of Argentina was solved, comparing the results obtained by the full space branch-and-bound method with those reported by the approximate algorithm.

The problem consists of 24 sub-regions representing original Argentinean provinces with corresponding demand of sugar and ethanol. The sub-regions and demand values corresponding to the first time period are shown in Table 1, whereas the demand for the remaining periods is provided as supplementary material. Distances between sub-regions were determined considering the capitals of the corresponding provinces and the main roads connecting these capitals. These data are listed in Table 2.

We assume that each sub-region has an associated sugar cane capacity. Particularly, sugar cane plantations are situated in five Argentinean provinces, whose production capacities are given in Table 3. The remaining regions have the option of importing sugar cane from these provinces, which may eventually lead to an increase in the transport operating cost. The minimum and maximum production capacities of each technology are listed in Table 4. The minimum and maximum storage capacities for liquid and solid materials are assumed to be 200 and 2 billion tons, respectively. The unit storage cost is assumed to be \$0.365/(ton·year) for all types of materials. Fixed and variable investment coefficients for different production and storage modes are listed in Tables 5 and 6, respectively. The prices for final products obtained from actual trading data are presented in Table 7. Unit production cost for sugar and ethanol are equal to \$265/ton and \$317/ton, respectively. The parameters used to calculate the capital and operating cost for different transportation modes can be found in Table 8. The minimum flow rate of each transportation mode is assumed to be equal to the minimum capacity of the corresponding transportation mode, whereas the maximum flow rates for heavy trucks, medium trucks and tanker trucks are 6.25, 6.25 and 6.00 million tons per year, respectively.

### 5.1. Computational performance of the “rolling horizon” approach as compared to the NPV-based MILP

To highlight the computational performance of the proposed “rolling horizon” algorithm as compared to a “full space” branch-and-bound method, nine example problems were solved maximizing NPV as single objective. Because the issue is to highlight the computational advantages, there is no need to apply the overall heuristic method to maximize the ROI.

The problems to be solved had different levels of complexity based on the length of the time horizon. All the models were written in GAMS (Rosenthal, 2008) and solved with the MILP solver CPLEX 12 on a HP Compaq DC5850 desktop PC with an AMD Phenom 8600B, 2.29 GHz triple-core processor, and 2.75 Gb of RAM.

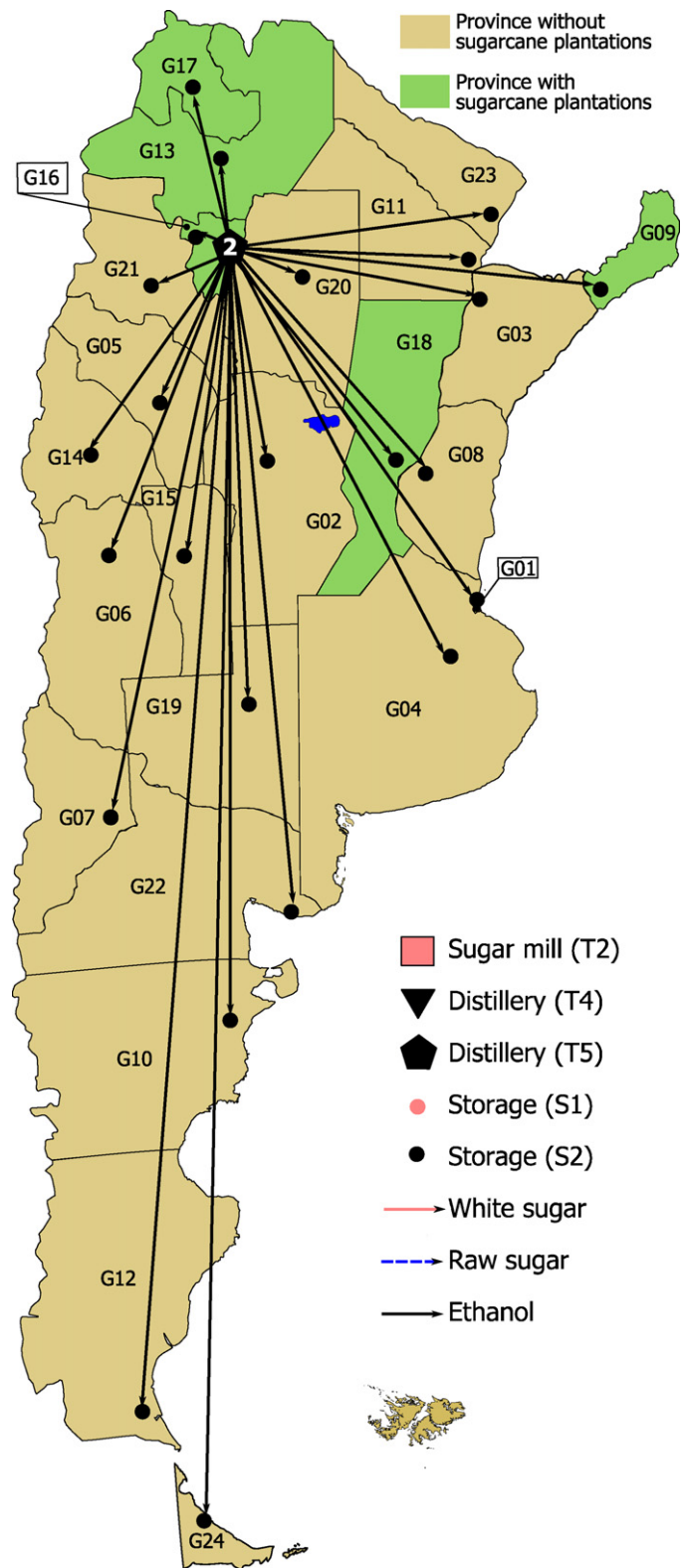


Fig. 16. Configuration of SC under low level of white sugar price.

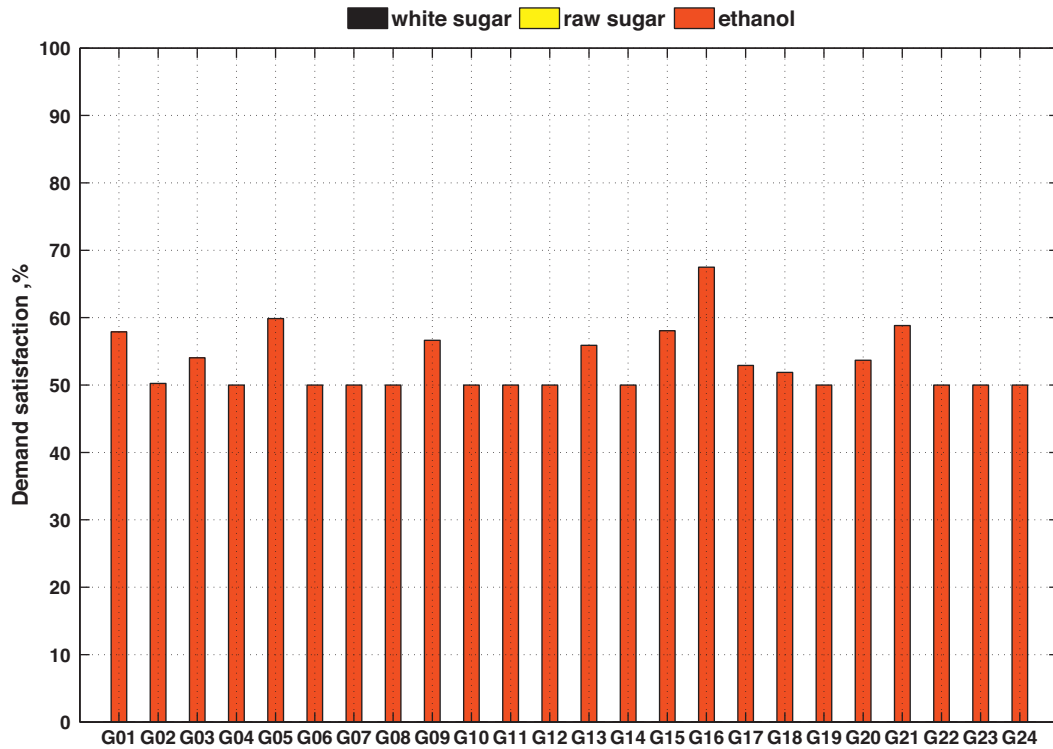


Fig. 17. Demand satisfaction level under low level of sugar price.

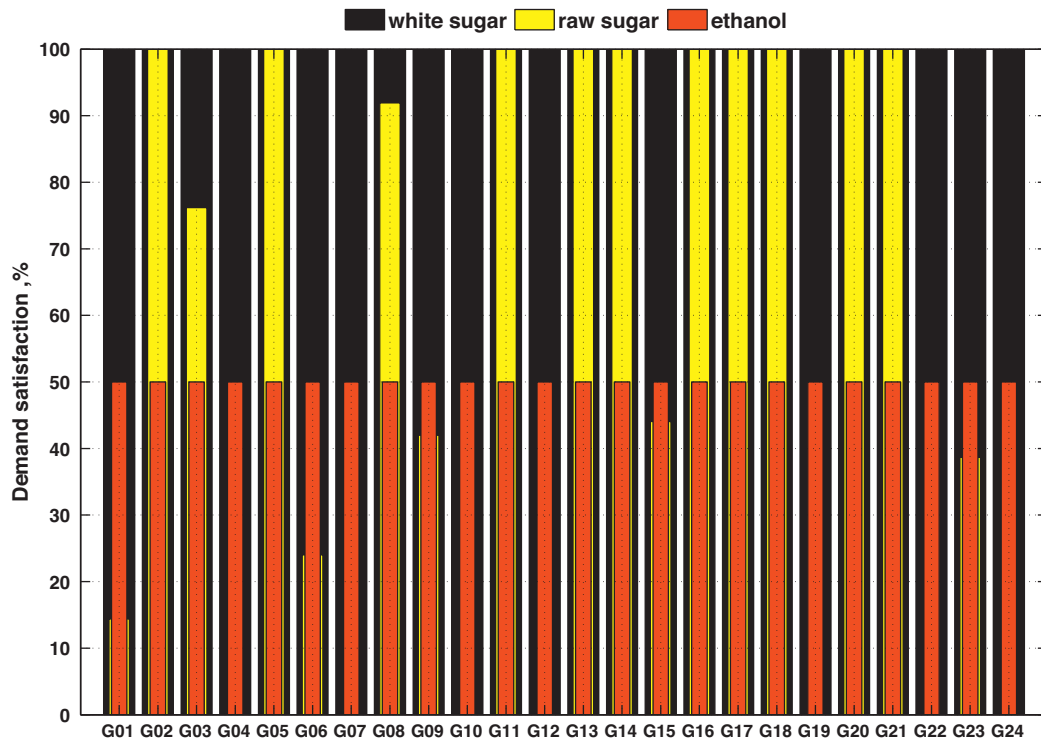


Fig. 18. Demand satisfaction level under low level of ethanol price.

Specifically, the “full space” and “rolling horizon” methods were applied to several problems with time horizons from 2 to 10 years. The upper bound on the capital investment was 1.5 billion \$ for all of them.

Figs. 4–12 show the lower and upper bounds provided by the “full space” method as a function of time. In the same figures, we have depicted the solutions calculated by the “rolling-horizon” algorithm using different optimality gaps in the sub-problems. As



**Table 10**  
Capital investments utilized with maximum ROI.

| Case               | FCI, \$            | NPV, \$       | ROI     |
|--------------------|--------------------|---------------|---------|
| Base level         | $1.77 \times 10^9$ | 479,217,967   | 0.1081  |
| High ethanol price | $1.86 \times 10^9$ | 868,467,640   | 0.1796  |
| Low ethanol price  | $1.74 \times 10^9$ | 151,473,075   | 0.0409  |
| High sugar price   | $1.77 \times 10^9$ | 1,375,331,563 | 0.2945  |
| Low sugar price    | $1.10 \times 10^9$ | −297,129,603  | −0.0924 |
| High fuel price    | $1.77 \times 10^9$ | 455,791,162   | 0.1031  |
| Low fuel price     | $1.79 \times 10^9$ | 503,390,346   | 0.1119  |

seen, for 2 and 4 time periods, the “full space” method performs better than the rolling horizon, whereas in the remaining cases, there is always at least one tuning of the “rolling-horizon” algorithm that outperforms CPLEX in terms of time (i.e., our algorithm provides solutions with less than 3% of optimality gap in shorter CPU times).

Table 9 provides the optimal solution (i.e., the solution with zero optimality gap) of each instance being solved along with the solutions calculated by the “rolling-horizon” method solving the sub-problems with different optimality gaps. Note that the model can only be solved to global optimality in some cases, whereas in others it is not possible to close the gap to zero after 43,200 of CPU time. Hence, the optimal results refer either to the global optimal solution (in those cases in which such a solution is identified before the time limit is exceeded) or to the solution attained after 43,200 of CPU time. As observed, the “rolling-horizon” algorithm provides in all the cases solutions with low optimality gaps (less than 3%).

## 5.2. Results for the case study

After proving the computational efficiency of the method, we next used the model to obtain valuable insight on the SC design problem for different plausible scenarios that differ in the cost data. We consider a three-year planning horizon assuming the input data given in Tables 7 and 8. A minimum demand satisfaction level constraint that forces the model to fulfill at least 50% of the ethanol demand in each sub-region was also included. Particularly, we solved the problem for the base case and compared the obtained results with the cases of low (50% below the base case level) and high levels (50% above the base case level) of fuel, sugar and ethanol prices.

For generating solutions close to the maximum ROI using our heuristic approach, we divided the interval  $[0, FCI]$  into 20 subintervals and maximized the NPV for different upper bounds on the capital investment that corresponded to the limits of these subintervals. From the obtained solutions, we identified the one with the largest ROI. The results of this analysis are presented in Table 10. The resulting ROI values for different levels of prices are depicted in Fig. 13.

As shown, ethanol and white sugar prices have the greatest impact on the ROI whereas the impact of the fuel price is rather low. The ROI and NPV take negative values in some cases because the model is forced to attain a minimum demand satisfaction level of ethanol of 50%, even if the production of this product is not profitable. This could be an important result for decision makers, calling for some subsidies or tax relief. Table 11 presents capital and operational expenditures as well as revenues for different prices. As observed, plant, storage and transportation capital costs have similar values. This is due to the small amount of production facilities and large number of storages and transportation links that must be established in the whole territory of Argentina to guarantee a minimum demand satisfaction level for ethanol of 50% in each Argentinean province. Regarding operating cost,

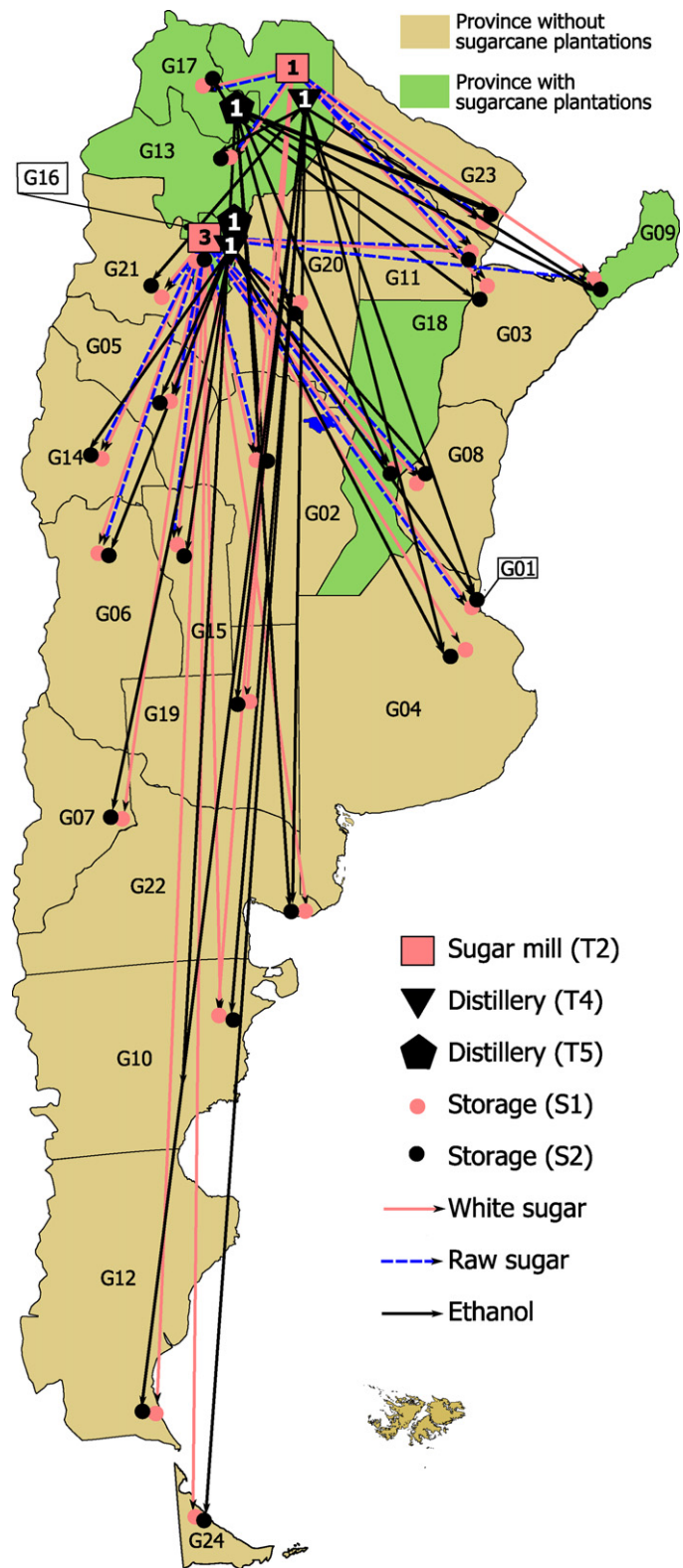


Fig. 19. Configuration of SC under high level of ethanol price.

landfill expenditures have the smallest share in the operating cost for all cases, and facility operating cost is ten times greater than transportation payments. Among the most profitable cases (high level of white sugar and ethanol price and low level of fuel price) the greatest value of revenue occurs with the increased price of white sugar.

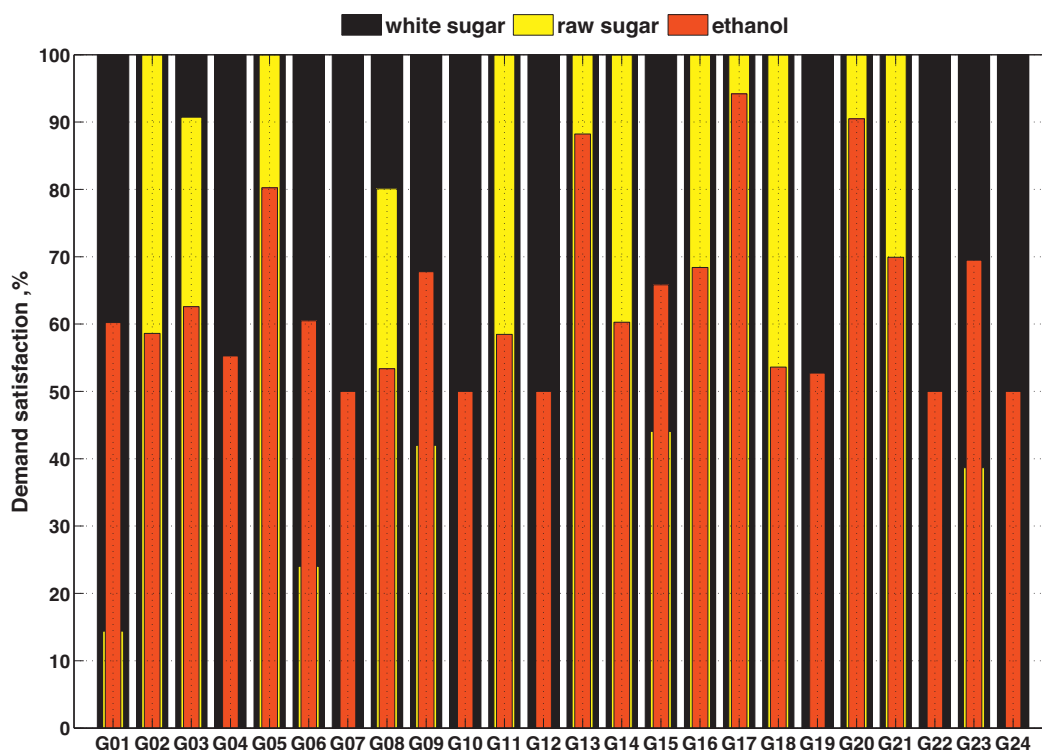


Fig. 20. Demand satisfaction level under high level of ethanol price.

Fig. 14 illustrates the SC configuration for the base case. The absence of sugar cane plantations in most of the Argentinean provinces results in a centralized SC that involves the establishment of production facilities only in Tucumán, Jujuy and Salta, which have inner sources of sugar cane. This configuration is motivated by the large amount of raw materials required for sugar and ethanol production, which would lead to prohibitive transportation cost if the plants were settled far away from the plantations. The resulting demand satisfaction level is shown in Fig. 15. As observed, most of the provinces, except Tucumán and a number of neighboring regions, attain the minimum possible ethanol supply, which indicates the unfavorable situation for ethanol in these regions compared to sugar.

We now show how the model responds to the changes on prices. We illustrate their effect on the optimal SC configuration and the way in which the model can be used to analyze situations that can be encountered in practice. The reduction of sugar price makes the model switch from the combined sugar-ethanol network to an exclusively bioethanol SC with 2 production plants that convert

sugar cane directly into ethanol (i.e., distillery T5). The SC configuration for low white sugar price is depicted in Fig. 16. Fig. 17 shows the demand satisfaction level in this case. The need to supply all regions with ethanol and a sugar cane deficit make that ethanol demand is not satisfied completely even in the provinces with their own sugar cane plantations.

The optimal SC configuration for the base level of the product prices remains optimal for the case of the increased sugar price. This happens because the ethanol demand satisfaction constraint results in that sugar cane is converted mainly in ethanol, and sugar factories have not enough amount of raw materials to expand sugar production even under very favorable conditions in the sugar market. Hence, there is no difference in SCs topology and demand satisfaction pattern between the base and high levels of sugar prices.

Fig. 18 depicts the demand satisfaction level under low price of ethanol. It shows that the distilleries produce only the minimum amount of ethanol necessary to attain a 50% of demand satisfaction. For this case the SC configuration is the same as in the base case.

**Table 11**  
Impact of fuel, sugar and ethanol prices on capital and operating costs.

| Case          | Capital cost, \$ |             |                      | Operating cost, \$ |               |                | Revenue, \$   |
|---------------|------------------|-------------|----------------------|--------------------|---------------|----------------|---------------|
|               | Plants           | Storages    | Transportation links | Disposal           | Facility      | Transportation |               |
| Fuel price    |                  |             |                      |                    |               |                |               |
| Low level     | 1,171,823,436    | 582,485,087 | 34,160,000           | 2,482,742          | 1,478,344,669 | 173,343,027    | 3,939,862,440 |
| Base level    | 1,154,384,264    | 582,485,087 | 33,560,000           | 2,408,644          | 1,459,984,820 | 208,941,020    | 3,905,368,643 |
| High level    | 1,157,272,391    | 582,485,087 | 32,635,000           | 2,388,156          | 1,454,908,384 | 239,818,010    | 3,895,831,223 |
| Sugar price   |                  |             |                      |                    |               |                |               |
| Low level     | 562,340,000      | 525,742,524 | 12,800,000           | 2,312,061          | 572,930,061   | 58,694,929     | 1,076,400,000 |
| Base level    | 1,154,384,264    | 582,485,087 | 33,560,000           | 2,408,644          | 1,459,984,820 | 208,941,020    | 3,905,368,643 |
| High level    | 1,154,384,264    | 582,485,087 | 33,560,000           | 2,408,644          | 1,459,984,820 | 208,941,020    | 5,319,719,295 |
| Ethanol price |                  |             |                      |                    |               |                |               |
| Low level     | 1,128,335,938    | 582,210,025 | 33,560,000           | 2,297,980          | 1,432,561,324 | 207,749,576    | 3,341,273,840 |
| Base level    | 1,154,384,264    | 582,485,087 | 33,560,000           | 2,408,644          | 1,459,984,820 | 208,941,020    | 3,905,368,643 |
| High level    | 1,239,355,122    | 585,161,472 | 34,530,000           | 2,736,842          | 1,541,324,478 | 213,160,522    | 4,672,929,399 |

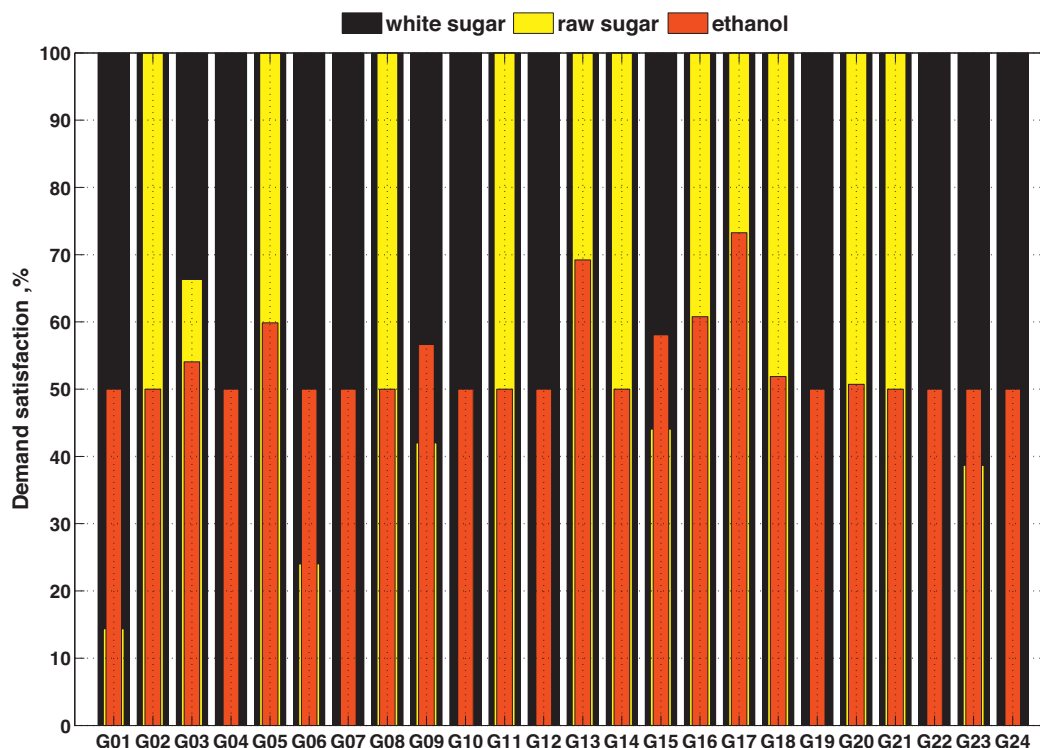


Fig. 21. Demand satisfaction level under high level of fuel price.

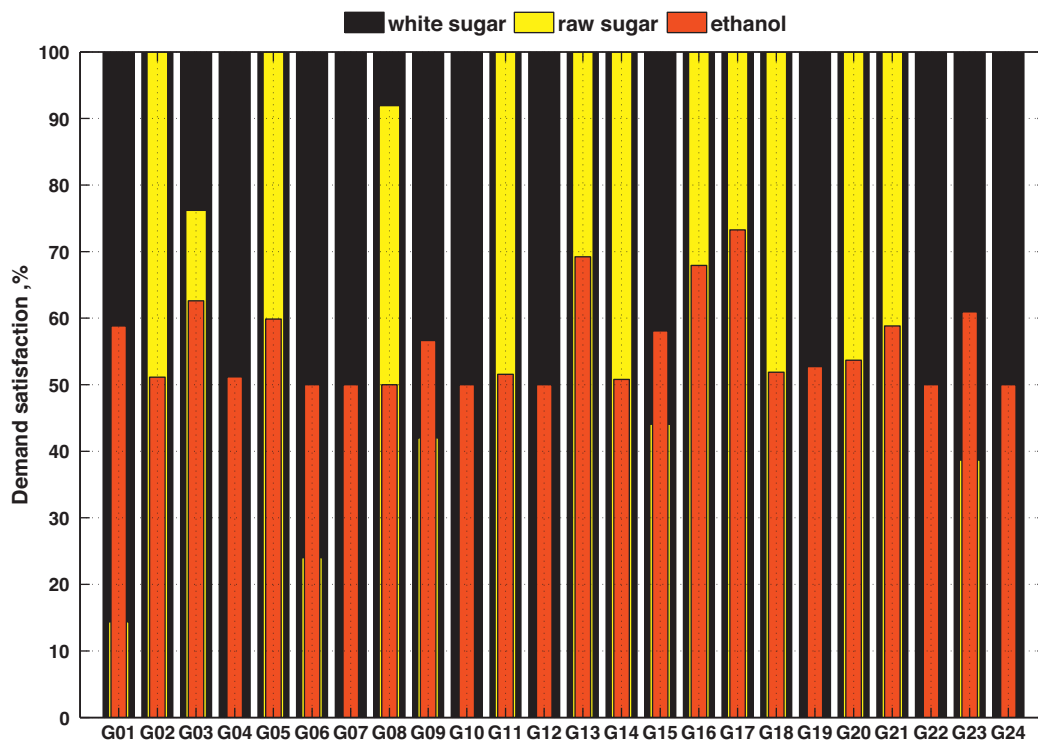


Fig. 22. Demand satisfaction level under low level of fuel price.

On the other hand, a 50% increase in the ethanol price increases the ethanol production and sugar cane consumption and leads to the establishment of a new distillery T5 in Tucumán and a shift from technology T5 to the pair T2–T4 in Salta. The SC configuration under high level of ethanol price is depicted in Fig. 19. Fig. 20 depicts the demand satisfaction level under high level of ethanol price. This plot

shows that a 50%-increase of ethanol price results in a significant growth of the demand satisfaction level of ethanol and a shrinkage in sugar production.

With regard to the fuel price, we note that this parameter has the lowest influence on the NPV, and its fluctuations mainly result in changes of production capacity but do not affect the supply chain

configuration that remains the same as under the base level of prices. Figs. 21 and 22 show the demand satisfaction level under high and low level of fuel price, respectively. As shown, a 50%-decrease of fuel price favors the ethanol production leading to higher ethanol demand satisfaction levels in the distant Argentinean provinces

## 6. Conclusions

In this work we have addressed the optimal design and planning of integrated sugar/ethanol SCs. The design task was formulated as a mixed-integer programming problem that seeks to maximize the ROI and that is approximated by solving a series of MILPs that maximize the NPV for different fixed capital investment values. To overcome the large computational burden of solving these MILPs, we proposed an approximation algorithm based on a “rolling horizon” strategy. The capabilities of the proposed mathematical model and solution strategy were shown through a case study based on the Argentinean sugar cane industry.

On the computational side, the “rolling horizon” algorithm provided near optimal solutions (i.e., with less than 3% of optimality gap) in a fraction of the time spent by CPLEX. A sensitivity

analysis was also conducted to study the impact that the prices of fuel, ethanol and sugar have on the economic performance and structural configuration of the SC. It was shown that sugar price has the greatest influence on the structure and performance of the integrated ethanol/sugar supply chain. The SC configurations obtained in all the cases are rather centralized, involving the establishment of few production facilities close to the sugar cane plantations. The systematic tool presented in this article aims to facilitate the task of decision makers from the viewpoints of analysis, improvement and optimization of distributed facilities.

## Acknowledgments

The authors wish to acknowledge support from the CON-ICET (Argentina), the Spanish Ministry of Education and Science (DPI2008-04099/DPI, CTQ2009-14420 and ENE2008-06687-C02-01), and the Spanish Ministry of External Affairs (projects A/8502/07, A/023551/09 and HS2007-0006).

## Appendix A. Demand data

| Sub-region | White sugar | Raw sugar | Ethanol |
|------------|-------------|-----------|---------|
| 1st year   |             |           |         |
| G01        | 53,644      | 40,249    | 60,394  |
| G02        | 84,280      | 62,874    | 108,680 |
| G03        | 17,848      | 17,556    | 31,812  |
| G04        | 276,077     | 292,334   | 342,248 |
| G05        | 11,647      | 3038      | 7860    |
| G06        | 64,097      | 11,366    | 70,309  |
| G07        | 22,832      | 5188      | 19,950  |
| G08        | 25,634      | 11,980    | 38,342  |
| G09        | 25,365      | 11,358    | 30,888  |
| G10        | 8193        | 7975      | 8622    |
| G11        | 25,587      | 11,709    | 31,952  |
| G12        | 5259        | 2243      | 5255    |
| G13        | 25,889      | 15,700    | 33,242  |
| G14        | 12,074      | 8440      | 27,652  |
| G15        | 17,568      | 2599      | 9377    |
| G16        | 46,365      | 18,572    | 79,890  |
| G17        | 22,286      | 7753      | 17,350  |
| G18        | 62,814      | 36,975    | 89,866  |
| G19        | 10,321      | 2777      | 9133    |
| G20        | 29,559      | 6875      | 26,944  |
| G21        | 10,793      | 4233      | 8375    |
| G22        | 8576        | 7842      | 14,485  |
| G23        | 22,035      | 5533      | 19,958  |
| G24        | 3852        | 2224      | 3890    |
| 2nd year   |             |           |         |
| G01        | 55,458      | 23,072    | 107,728 |
| G02        | 96,928      | 15,136    | 66,945  |
| G03        | 26,914      | 6959      | 39,482  |
| G04        | 690,366     | 202,816   | 495,091 |
| G05        | 13,053      | 6469      | 7866    |
| G06        | 56,074      | 12,265    | 62,488  |
| G07        | 15,706      | 6748      | 13,828  |
| G08        | 24,062      | 15,149    | 34,272  |
| G09        | 36,053      | 16,195    | 21,359  |
| G10        | 17,035      | 4826      | 17,895  |
| G11        | 17,264      | 10,214    | 9900    |
| G12        | 4824        | 1430      | 8731    |
| G13        | 37,737      | 13,325    | 23,540  |
| G14        | 24,968      | 13,342    | 26,827  |
| G15        | 10,067      | 5931      | 14,834  |
| G16        | 24,406      | 12,927    | 40,222  |
| G17        | 18,261      | 6264      | 10,412  |
| G18        | 49,098      | 34,633    | 90,737  |
| G19        | 7760        | 4845      | 8755    |
| G20        | 18,144      | 5567      | 28,084  |
| G21        | 6333        | 4245      | 7301    |
| G22        | 6422        | 7554      | 16,559  |
| G23        | 9620        | 9249      | 12,789  |

| Sub-region | White sugar | Raw sugar | Ethanol |
|------------|-------------|-----------|---------|
| G24        | 3413        | 1035      | 2170    |
| 3rd year   |             |           |         |
| G01        | 59,180      | 34,173    | 100,186 |
| G02        | 88,651      | 52,658    | 102,458 |
| G03        | 32,935      | 14,046    | 23,319  |
| G04        | 618,341     | 208,166   | 435,812 |
| G05        | 10,195      | 4798      | 13,662  |
| G06        | 41,832      | 27,447    | 39,005  |
| G07        | 12,648      | 6073      | 15,545  |
| G08        | 20,107      | 20,137    | 35,143  |
| G09        | 33,125      | 11,004    | 43,606  |
| G10        | 12,678      | 3800      | 17,819  |
| G11        | 19,143      | 15,705    | 29,725  |
| G12        | 4797        | 2679      | 4121    |
| G13        | 32,798      | 13,881    | 45,252  |
| G14        | 15,404      | 4286      | 13,037  |
| G15        | 8660        | 4931      | 9591    |
| G16        | 58,951      | 14,898    | 56,302  |
| G17        | 16,247      | 8069      | 14,875  |
| G18        | 32,433      | 50,177    | 100,418 |
| G19        | 11,106      | 3864      | 10,686  |
| G20        | 20,912      | 9453      | 23,443  |
| G21        | 8316        | 2965      | 4763    |
| G22        | 10,287      | 6759      | 14,577  |
| G23        | 12,048      | 9136      | 9165    |
| G24        | 2971        | 1430      | 1782    |
| 4th year   |             |           |         |
| G01        | 81,041      | 37,553    | 106,659 |
| G02        | 82,537      | 49,586    | 142,621 |
| G03        | 24,431      | 9003      | 21,211  |
| G04        | 452,336     | 175,920   | 433,350 |
| G05        | 10,352      | 5807      | 8657    |
| G06        | 54,661      | 24,024    | 20,394  |
| G07        | 10,726      | 9004      | 13,475  |
| G08        | 22,663      | 16,499    | 26,419  |
| G09        | 49,358      | 10,011    | 50,260  |
| G10        | 12,714      | 4271      | 15,163  |
| G11        | 32,203      | 11,762    | 19,996  |
| G12        | 2335        | 2065      | 5685    |
| G13        | 26,105      | 20,109    | 27,515  |
| G14        | 24,708      | 7233      | 23,561  |
| G15        | 10,183      | 5466      | 14,293  |
| G16        | 36,335      | 17,611    | 63,779  |
| G17        | 25,468      | 5588      | 24,870  |
| G18        | 77,247      | 48,772    | 96,126  |
| G19        | 6889        | 3701      | 9886    |
| G20        | 14,814      | 8601      | 13,183  |
| G21        | 6363        | 3899      | 12,756  |
| G22        | 14,532      | 4925      | 20,775  |

| Sub-region | White sugar | Raw sugar | Ethanol | Sub-region | White sugar | Raw sugar | Ethanol |
|------------|-------------|-----------|---------|------------|-------------|-----------|---------|
| G23        | 12,865      | 8755      | 15,089  | 8th year   |             |           |         |
| G24        | 4507        | 1442      | 548     | G01        | 77,585      | 22,353    | 75,116  |
| 5th year   |             |           |         | G02        | 60,651      | 35,034    | 93,484  |
| G01        | 90,436      | 57,265    | 45,973  | G03        | 21,598      | 12,804    | 27,094  |
| G02        | 116,148     | 43,967    | 75,119  | G04        | 589,705     | 136,193   | 672,791 |
| G03        | 22,863      | 7206      | 35,502  | G05        | 8060        | 6638      | 7869    |
| G04        | 527,709     | 234,621   | 402,829 | G06        | 45,772      | 29,352    | 43,579  |
| G05        | 12,864      | 5562      | 3681    | G07        | 11,444      | 5579      | 18,363  |
| G06        | 65,022      | 22,279    | 49,087  | G08        | 27,791      | 19,832    | 28,098  |
| G07        | 18,420      | 3426      | 14,455  | G09        | 23,466      | 14,446    | 41,204  |
| G08        | 36,948      | 10,959    | 28,498  | G10        | 17,446      | 5687      | 15,949  |
| G09        | 23,199      | 14,015    | 34,941  | G11        | 32,335      | 12,262    | 33,185  |
| G10        | 12,668      | 3150      | 9478    | G12        | 10,223      | 1883      | 4010    |
| G11        | 29,923      | 18,584    | 43,724  | G13        | 25,940      | 17,717    | 39,359  |
| G12        | 7568        | 2013      | 3750    | G14        | 14,105      | 4675      | 25,762  |
| G13        | 26,388      | 14,973    | 27,764  | G15        | 12,560      | 6126      | 12,283  |
| G14        | 19,210      | 9292      | 21,302  | G16        | 33,300      | 26,912    | 47,714  |
| G15        | 10,354      | 5268      | 12,824  | G17        | 14,549      | 10,084    | 23,989  |
| G16        | 40,946      | 26,396    | 36,171  | G18        | 78,210      | 35,304    | 115,779 |
| G17        | 11,299      | 7951      | 12,616  | G19        | 8305        | 4328      | 7250    |
| G18        | 105,312     | 33,214    | 102,151 | G20        | 31,068      | 15,178    | 24,256  |
| G19        | 4637        | 3536      | 6745    | G21        | 6422        | 4269      | 11,348  |
| G20        | 16,971      | 12,096    | 26,892  | G22        | 28,174      | 5267      | 13,268  |
| G21        | 8147        | 3162      | 7442    | G23        | 9430        | 6776      | 11,364  |
| G22        | 14,457      | 7242      | 18,523  | G24        | 1810        | 1816      | 2790    |
| G23        | 14,525      | 9671      | 15,193  | 9th year   |             |           |         |
| G24        | 3442        | 1514      | 3022    | G01        | 61,168      | 43,340    | 40,564  |
| 6th year   |             |           |         | G02        | 80,033      | 41,837    | 115,077 |
| G01        | 37,848      | 41,331    | 61,292  | G03        | 21,797      | 12,515    | 28,055  |
| G02        | 79,839      | 25,510    | 85,563  | G04        | 264,304     | 200,822   | 505,320 |
| G03        | 32,855      | 16,495    | 34,354  | G05        | 10,181      | 6137      | 486     |
| G04        | 350,540     | 236,424   | 655,308 | G06        | 53,675      | 30,418    | 67,046  |
| G05        | 8370        | 3602      | 12,712  | G07        | 9534        | 7554      | 14,329  |
| G06        | 46,584      | 26,398    | 53,566  | G08        | 31,868      | 14,063    | 17,189  |
| G07        | 16,892      | 7440      | 23,587  | G09        | 30,310      | 12,046    | 36,014  |
| G08        | 27,271      | 9900      | 35,873  | G10        | 12,923      | 7355      | 10,558  |
| G09        | 22,653      | 11,804    | 42,209  | G11        | 19,663      | 16,414    | 48,901  |
| G10        | 8738        | 6144      | 17,186  | G12        | 5303        | 2316      | 9022    |
| G11        | 31,398      | 20,102    | 7421    | G13        | 34,221      | 10,015    | 23,035  |
| G12        | 5046        | 3306      | 6200    | G14        | 13,204      | 14,507    | 15,897  |
| G13        | 24,887      | 5190      | 34,655  | G15        | 8287        | 5250      | 12,466  |
| G14        | 18,112      | 8054      | 22,085  | G16        | 37,992      | 12,695    | 35,650  |
| G15        | 7765        | 5879      | 14,333  | G17        | 27,519      | 10,949    | 15,357  |
| G16        | 43,790      | 18,939    | 41,081  | G18        | 57,498      | 52,188    | 117,496 |
| G17        | 22,957      | 8194      | 17,907  | G19        | 7123        | 4435      | 10,312  |
| G18        | 95,156      | 40,275    | 103,366 | G20        | 17,120      | 15,918    | 28,450  |
| G19        | 2589        | 4284      | 9986    | G21        | 6321        | 4036      | 12,418  |
| G20        | 35,656      | 15,878    | 25,662  | G22        | 15,344      | 4745      | 19,232  |
| G21        | 9399        | 6479      | 7364    | G23        | 11,604      | 9085      | 8667    |
| G22        | 3437        | 9150      | 16,379  | G24        | 4371        | 1855      | 3400    |
| G23        | 17,489      | 8704      | 15,883  | 10th year  |             |           |         |
| G24        | 822         | 2579      | 2582    | G01        | 32,748      | 45,740    | 106,252 |
| 7th year   |             |           |         | G02        | 37,934      | 43,025    | 101,691 |
| G01        | 70,019      | 35,348    | 91,848  | G03        | 32,081      | 9455      | 28,496  |
| G02        | 92,488      | 54,416    | 81,006  | G04        | 262,056     | 214,018   | 418,869 |
| G03        | 20,019      | 19,429    | 33,165  | G05        | 10,616      | 4530      | 8762    |
| G04        | 269,807     | 115,749   | 495,853 | G06        | 56,416      | 29,465    | 36,161  |
| G05        | 10,035      | 2439      | 12,378  | G07        | 7920        | 9350      | 14,600  |
| G06        | 68,584      | 29,961    | 43,254  | G08        | 27,751      | 17,284    | 30,577  |
| G07        | 16,636      | 8694      | 20,569  | G09        | 23,619      | 22,553    | 29,771  |
| G08        | 13,324      | 18,070    | 40,562  | G10        | 13,940      | 8626      | 13,222  |
| G09        | 28,148      | 17,246    | 20,565  | G11        | 11,035      | 23,497    | 28,579  |
| G10        | 5804        | 6238      | 12,888  | G12        | 8965        | 3376      | 9916    |
| G11        | 6039        | 9934      | 23,552  | G13        | 33,963      | 14,753    | 20,669  |
| G12        | 6515        | 2658      | 5132    | G14        | 9150        | 8826      | 25,143  |
| G13        | 41,455      | 13,421    | 29,086  | G15        | 12,940      | 7330      | 11,127  |
| G14        | 21,249      | 8959      | 15,008  | G16        | 51,390      | 19,344    | 44,512  |
| G15        | 9197        | 3320      | 12,552  | G17        | 15,441      | 11,464    | 5051    |
| G16        | 59,223      | 16,115    | 43,151  | G18        | 94,839      | 9228      | 99,030  |
| G17        | 13,322      | 6847      | 26,592  | G19        | 8863        | 4993      | 9382    |
| G18        | 77,359      | 35,828    | 87,655  | G20        | 16,774      | 13,850    | 29,062  |
| G19        | 8435        | 3104      | 8679    | G21        | 12,074      | 6657      | 6582    |
| G20        | 20,236      | 8522      | 12,318  | G22        | 16,284      | 10,906    | 24,103  |
| G21        | 7375        | 575       | 12,537  | G23        | 10,322      | 7003      | 11,422  |
| G22        | 12,843      | 10,765    | 14,676  | G24        | 3657        | 680       | 3153    |
| G23        | 20,815      | 6128      | 14,248  |            |             |           |         |
| G24        | 5294        | 1569      | 3082    |            |             |           |         |



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